

The diagram illustrates the equivalence between paths and surfaces. It consists of two parts. On the left, a path from point X at the bottom to point Y at the top is shown as a single wavy line. Below it, the expression $\sum_{paths} e^{i \frac{mc}{\hbar} A_{xy}}$ is given. On the right, a surface from point X at the bottom to point Y at the top is shown as a wavy line with small circles representing vertices. Below it, the expression $\sum_{surfaces} e^{i \frac{mc}{\hbar} A_{xy}}$ is given. A double-headed purple arrow connects the two parts, indicating their equivalence. Below the right part, the equation $[A_{xy}] = cm$ is shown.

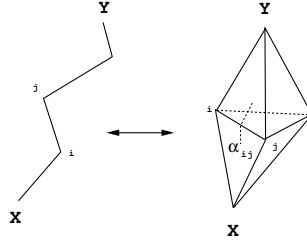
The Gonihedric Paradigm

Extensions of the Feynman Path Integral and of the Ising Model

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$$\mathbf{A}_{xy}$$

$$m \sum_{\langle ij \rangle} \lambda_{ij} \quad \longleftrightarrow \quad m \sum_{\langle ij \rangle} \lambda_{ij} (\pi - \alpha_{ij})^{\zeta}$$

The action A for random surfaces and for the random paths coincides when the surfaces degenerate to a single random path. The action involves the products of edge length $\lambda_{ij} = |x_i - x_j|$ times the corresponding deficit angle $|\pi - \alpha_{ij}|$ and the sum is over all edges

$$A = m \sum_{\langle ij \rangle} \lambda_{ij} |\pi - \alpha_{ij}|^{\zeta}.$$

The "gonihedric" paradigm is from two hellenic words $\gamma\omega\nu\nu'\alpha$ - the angle - and $\epsilon'\delta\rho\alpha$ - the side.

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