



NATIONAL CENTRE FOR  
SCIENTIFIC RESEARCH "DEMOKRITOS"  
INSTITUTE OF NUCLEAR AND PARTICLE PHYSICS



**H.F.R.I.**  
Hellenic Foundation for  
Research & Innovation

# Modelling uncertainties and prompt $b$ -jet identification in $t\bar{t}b\bar{b}$ with dilepton signatures at the LHC

**Giuseppe Bevilacqua**  
NCSR "Demokritos"

RADCOR 2023

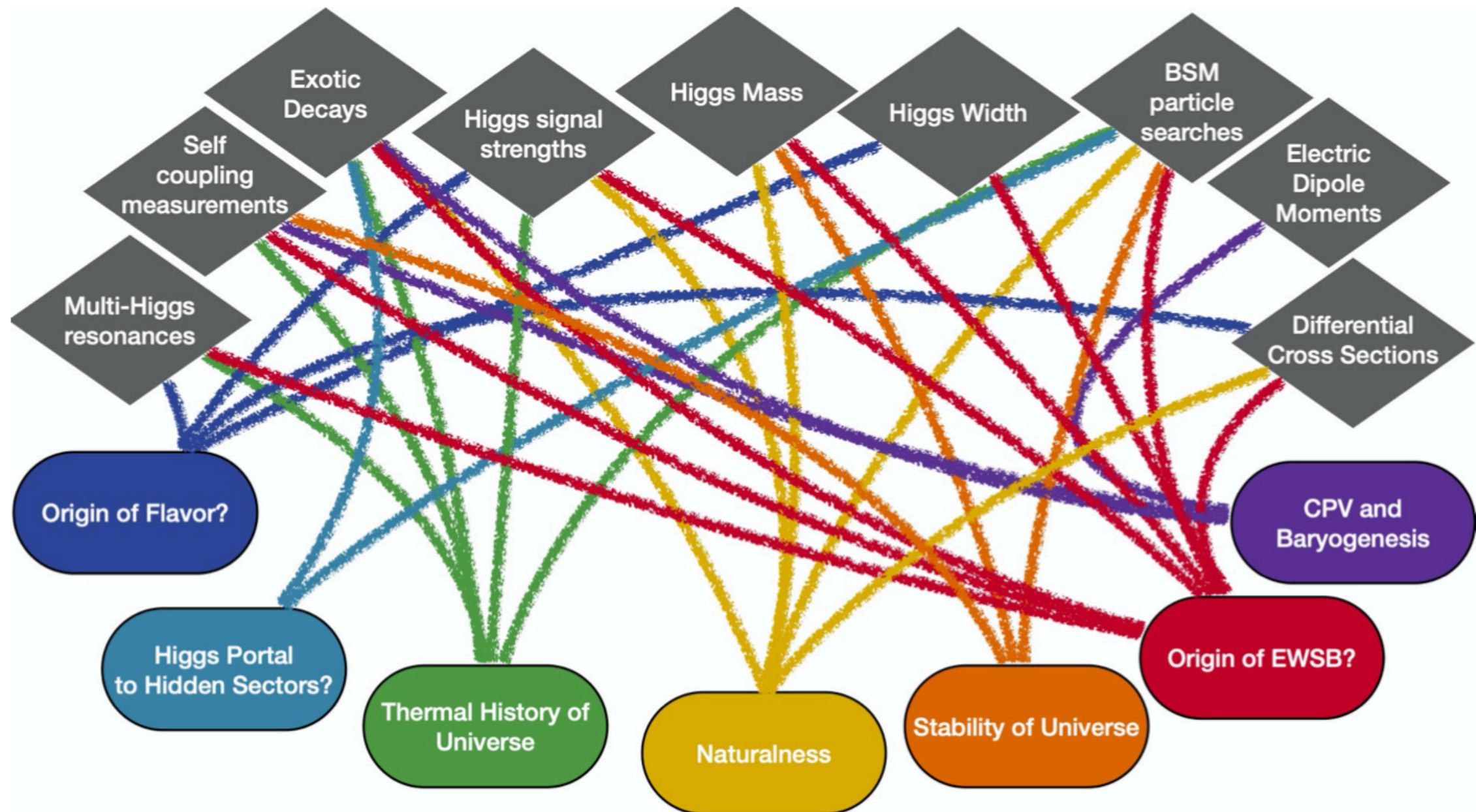
Crieff, Scotland  
May 30, 2023

Work in collaboration with H.Y. Bi, H.B. Hartanto, M.Kraus, M.Lupattelli and M.Worek

Based on: [JHEP 08 \(2021\) 008](#)      [Phys. Rev. D 107 \(2023\) 1](#)

# Motivation

- Understanding the properties of the SM Higgs boson is central to the physics program of the LHC (and of future colliders as well)

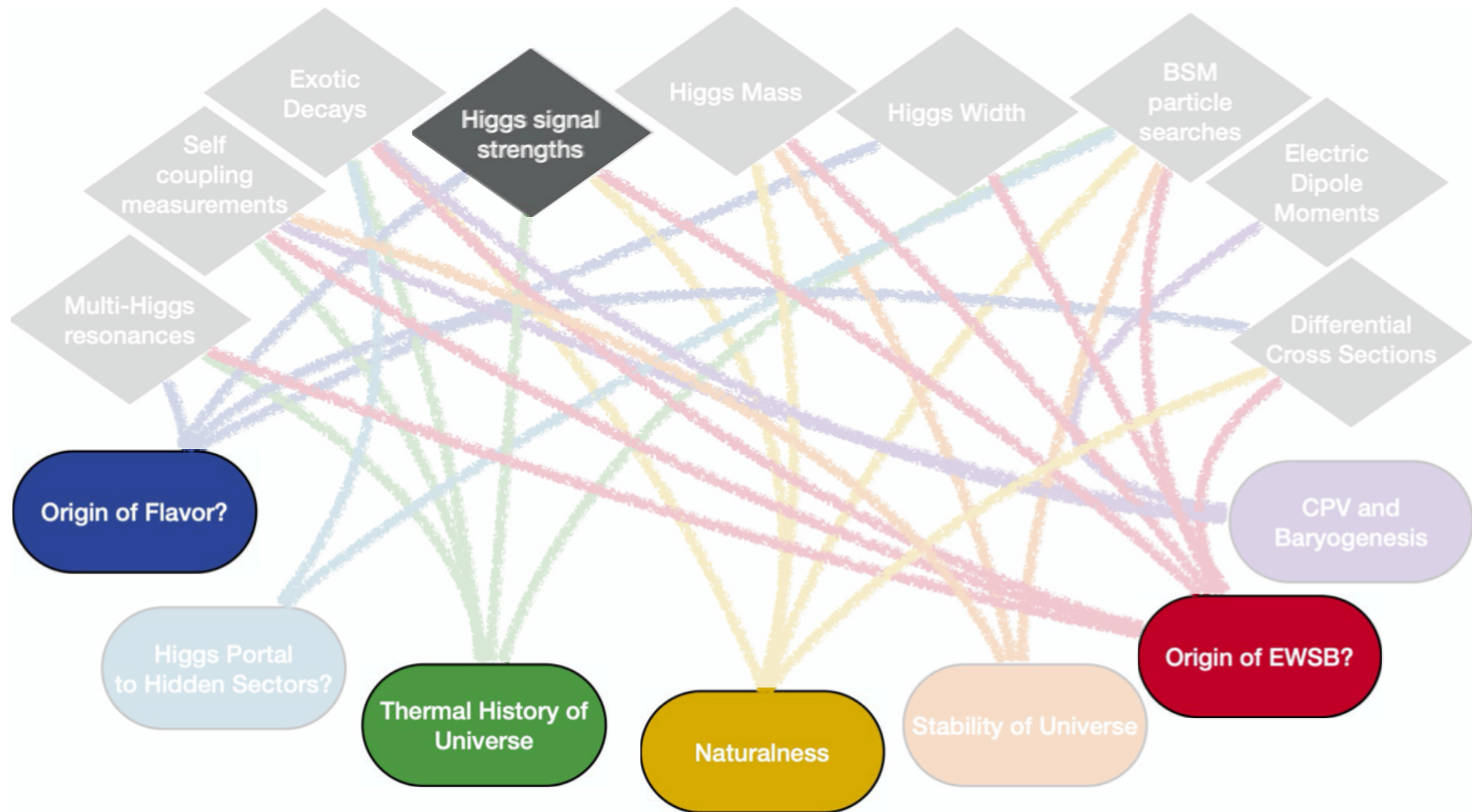


[2209.07510 \[hep-ph\]](#)

# Motivation

- Measurements of **Higgs signal strengths** can provide stringent tests of the SM
- BSM physics can manifest through **coupling modifiers** ( $\kappa$ ) with effects up to few %

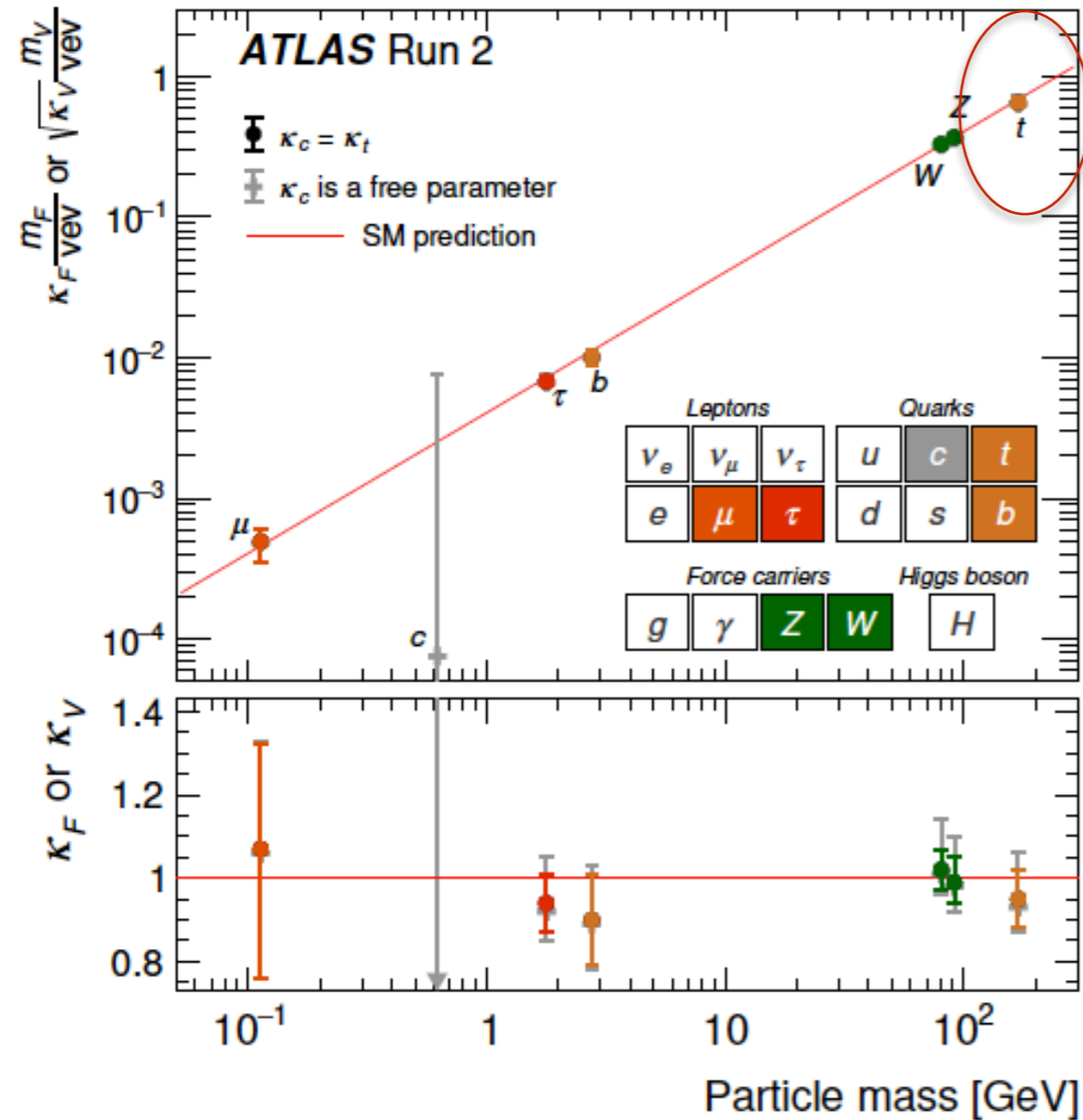
↪ Talk by Sinead Farrington



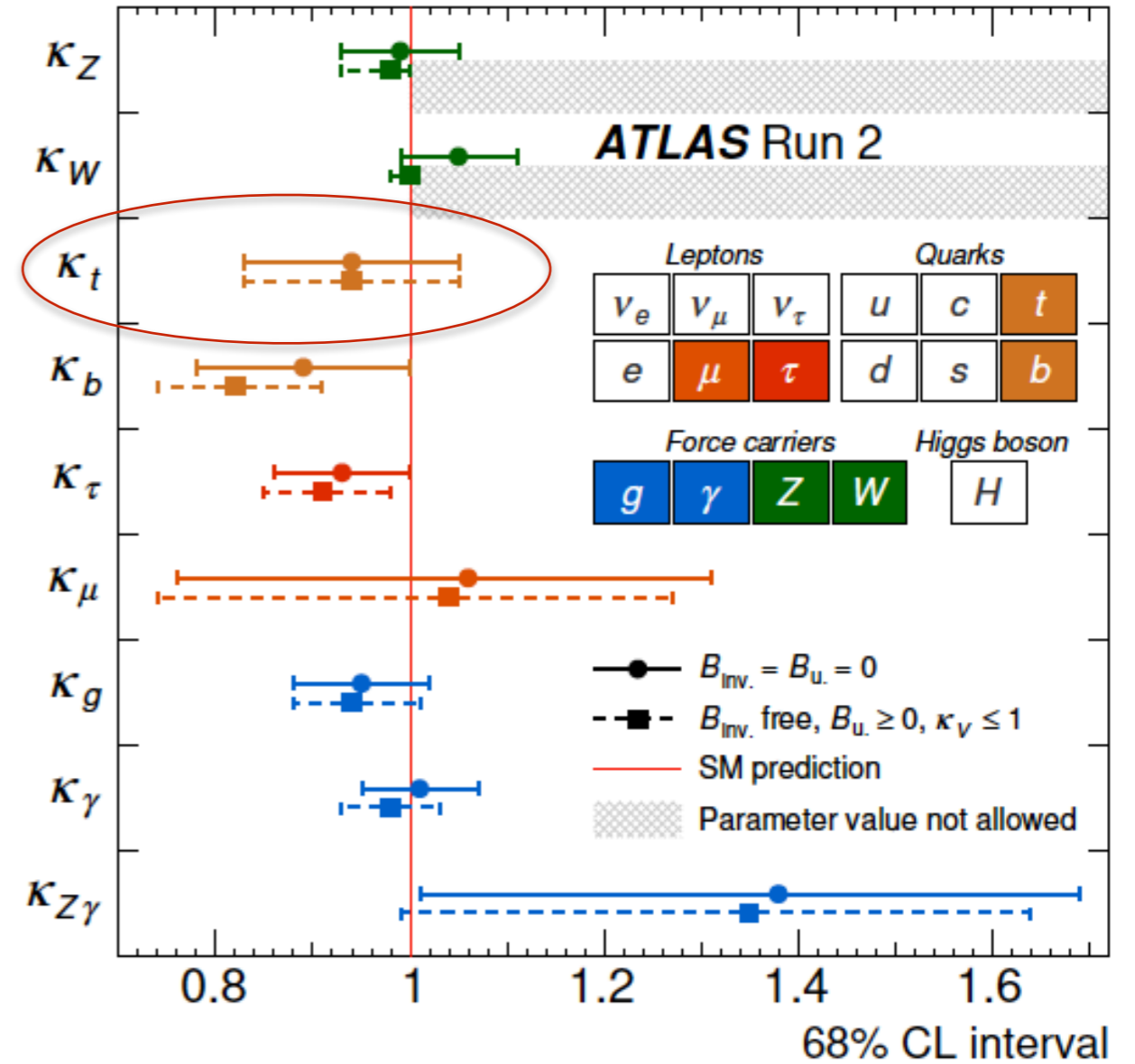
[2209.07510 \[hep-ph\]](https://arxiv.org/abs/2209.07510)

# Higgs coupling measurements

- Legacy results from the LHC Run 2



[ATLAS, [Nature 607 \(2022\) 7917, 52-59](#)]

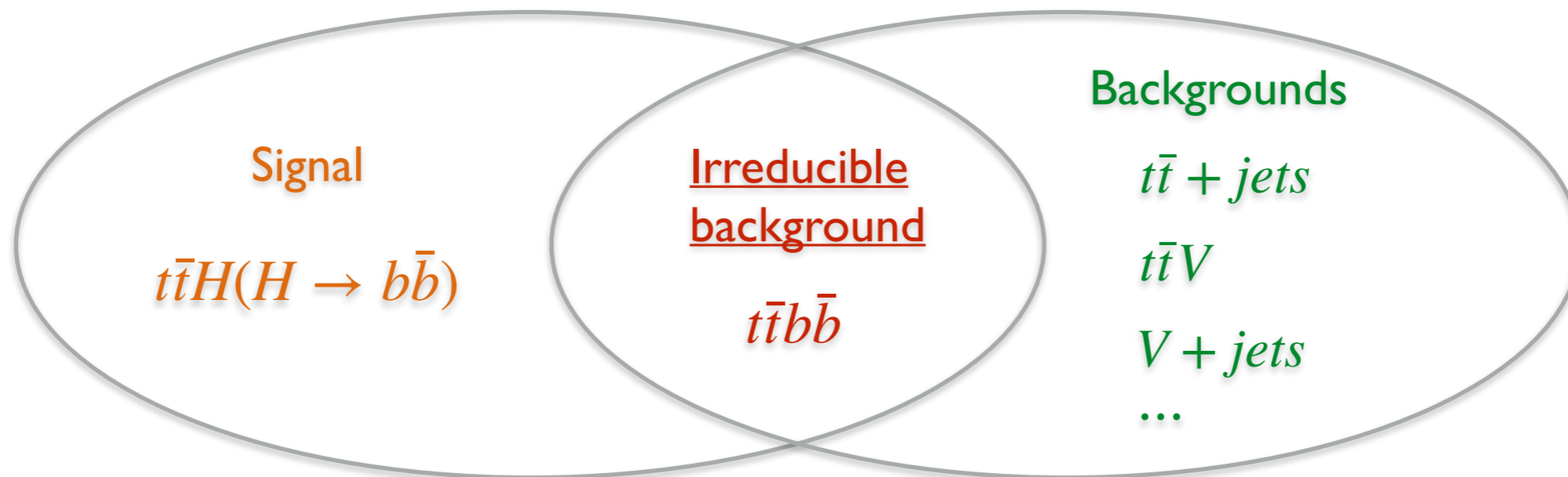


# Why $t\bar{t}H(H \rightarrow b\bar{b})$ ?

- Top-quark Yukawa coupling is the largest among SM particles
- $pp \rightarrow t\bar{t}H$  has direct sensitivity to top-quark Yukawa coupling at LHC
- $H \rightarrow b\bar{b}$  is the decay channel with the largest Branching Ratio (  $\sim 58\%$  )

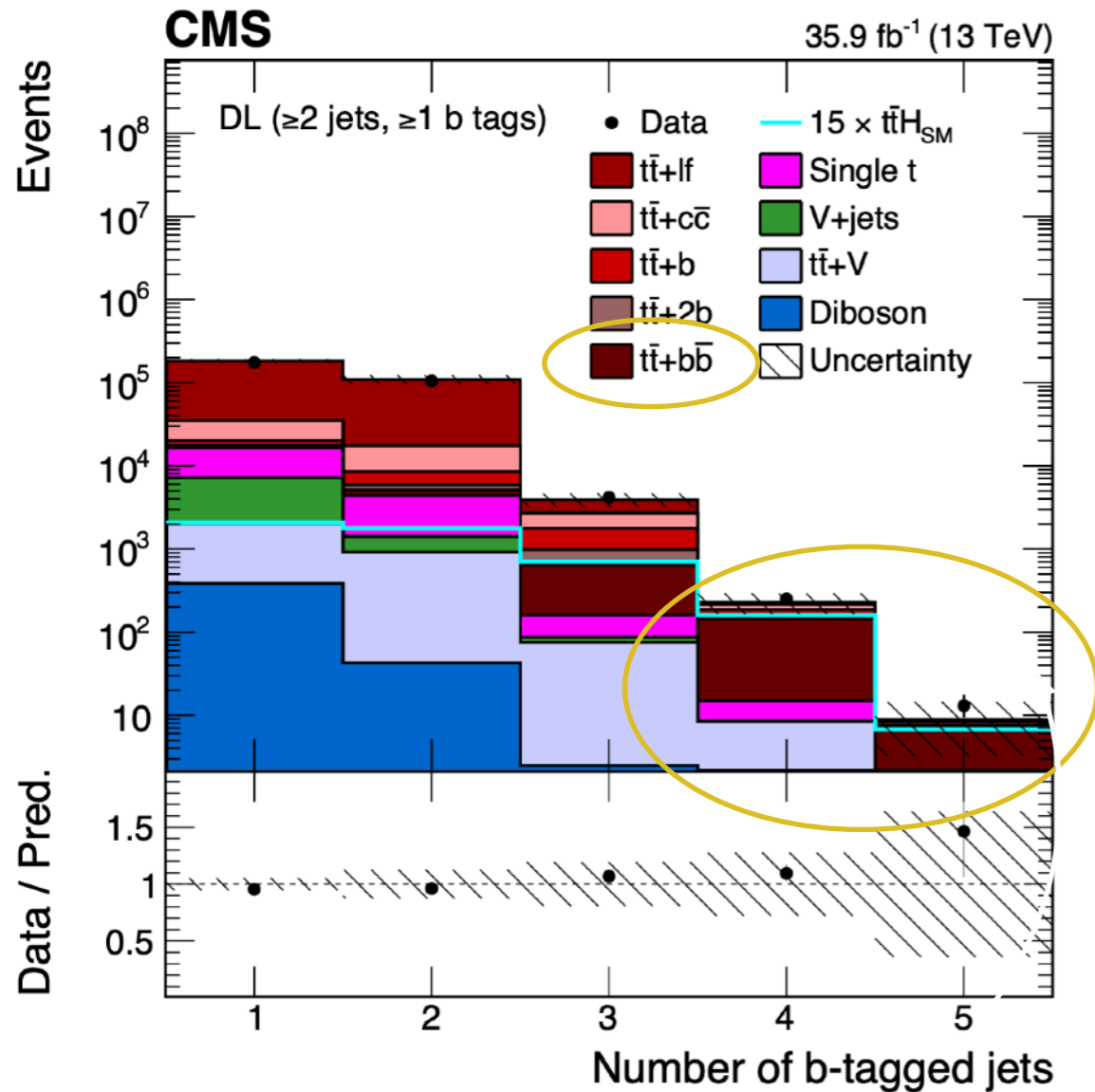
↪ Talk by Chiara Savoini

However  $pp \rightarrow t\bar{t}H(H \rightarrow b\bar{b})$  is a tiny signal in a huge QCD background



# $t\bar{t}b\bar{b}$ : theoretical challenges

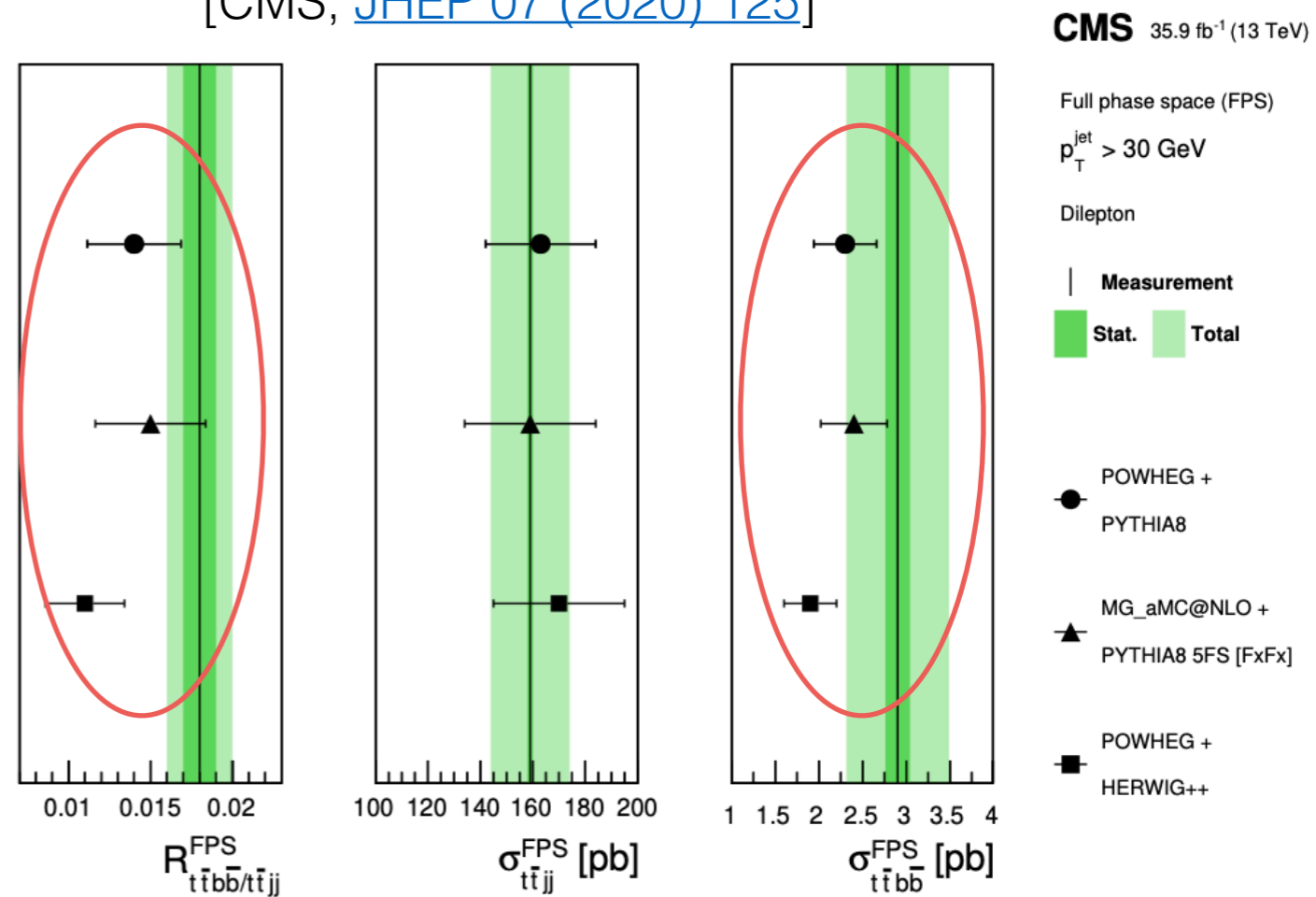
[CMS, [JHEP 03 \(2019\) 026](#)]



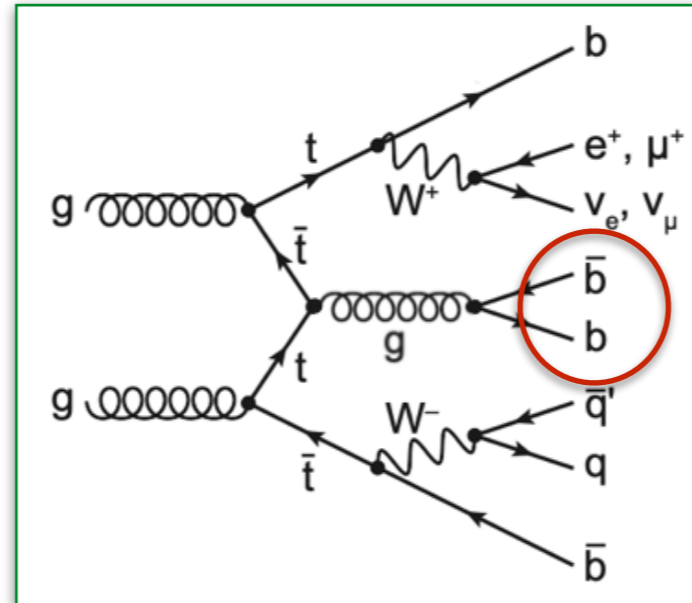
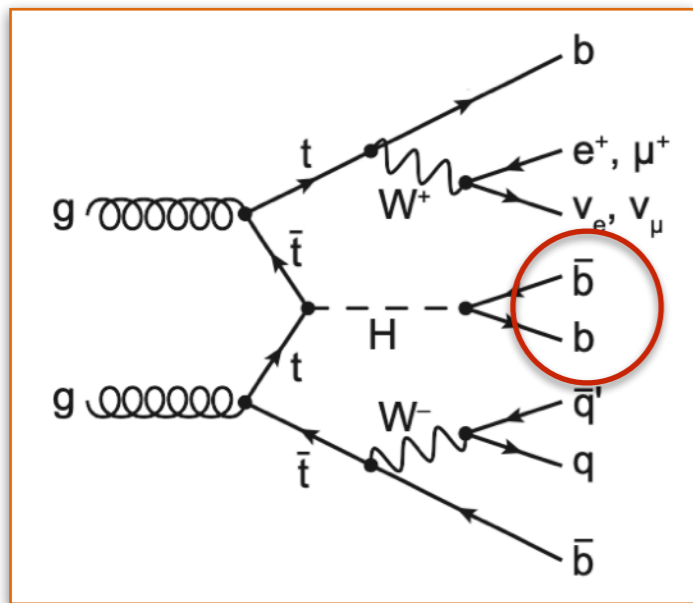
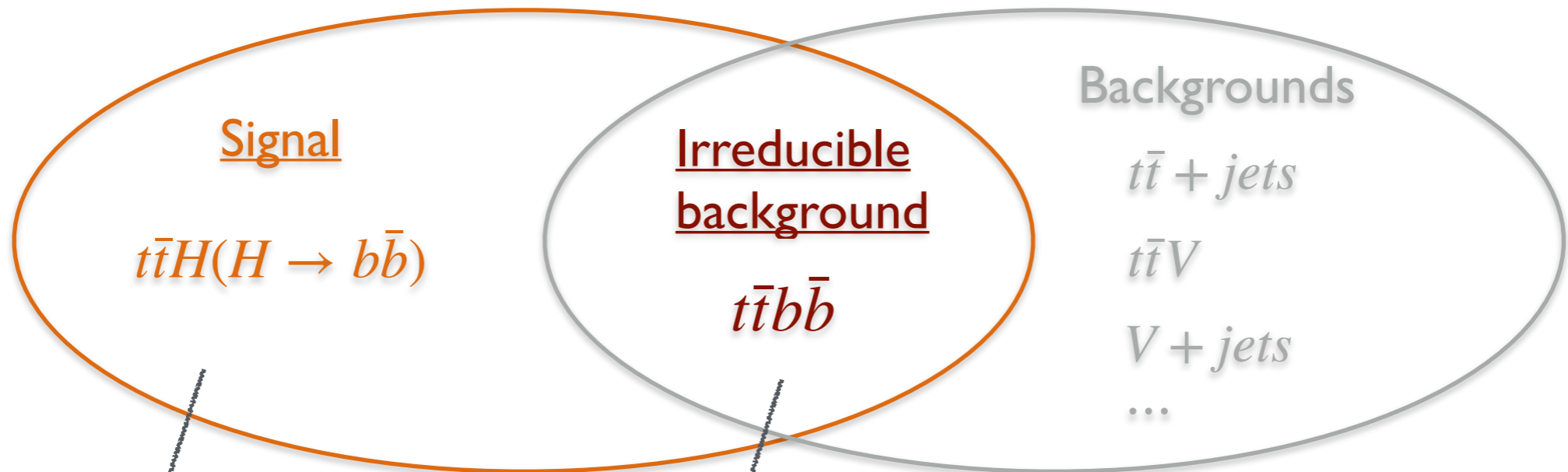
- $t\bar{t}b\bar{b}$ : main background to  $t\bar{t}H(H \rightarrow b\bar{b})$  for  $N_{bjets} \geq 4$

- Slight tension with data reported in  $\sigma(t\bar{t}b\bar{b})$  and in  $\mathcal{R} = \frac{\sigma(t\bar{t}b\bar{b})}{\sigma(t\bar{t}jj)}$

[CMS, [JHEP 07 \(2020\) 125](#)]



# $t\bar{t}b\bar{b}$ : prompt $b$ -jet identification



$$t \rightarrow W^+ b \quad \bar{t} \rightarrow W^- \bar{b} \quad H \rightarrow b\bar{b}$$

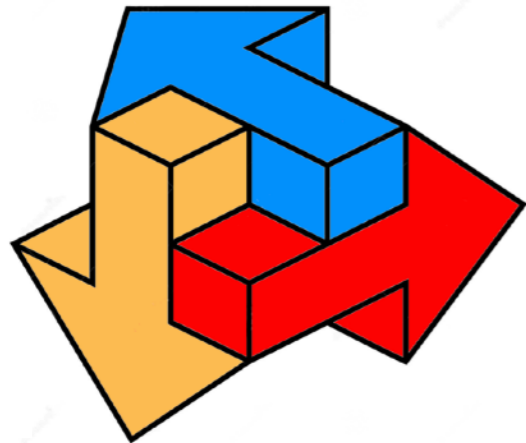
$$t \rightarrow W^+ b \quad \bar{t} \rightarrow W^- \bar{b} \quad g \rightarrow b\bar{b}$$

## Combinatorial background:

- challenges in top reconstruction & “prompt  $b$ -jet” identification
- smearing of Higgs peak in  $M(b\bar{b})$  distribution

# Avenues to precision

Higher orders

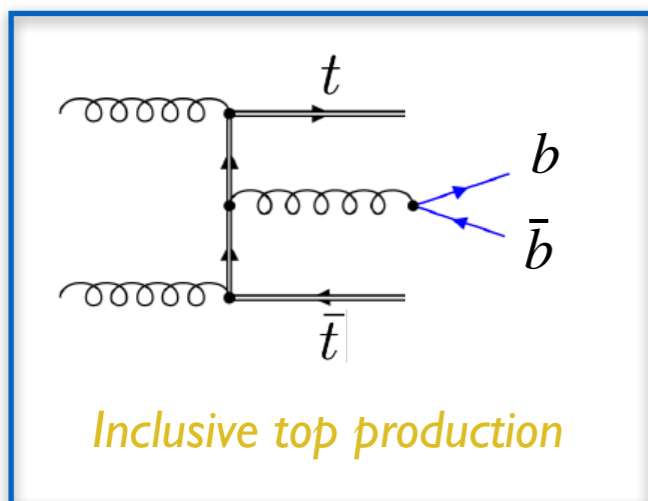


Shower & hadr.

Resonant structures

- Accurate predictions for *inclusive production rates*
- General idea on the impact of QCD corrections to  $t\bar{t}b\bar{b}$  production
- Global view on the size of dominant theory uncertainties

State of the art: **NLO QCD**



$$pp \rightarrow t\bar{t}b\bar{b}$$

Bredenstein, Denner, Dittmaier, Pozzorini '08 '09  
GB, Czakon, Papadopoulos, Pittau, Worek '09  
Denner, Dittmaier, Kallweit, Pozzorini '10  
Worek '12

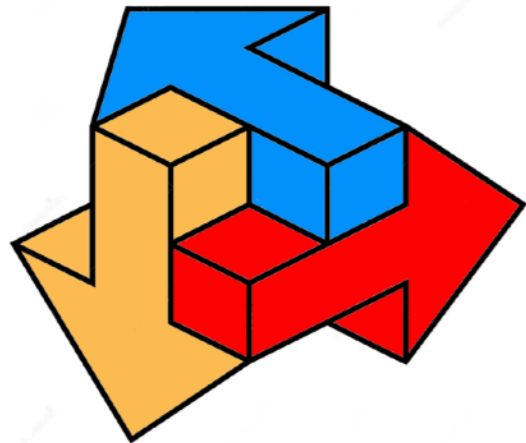
$$pp \rightarrow t\bar{t}b\bar{b}j$$

Buccioni, Kallweit, Pozzorini, Zoller '19



# Avenues to precision

Higher orders

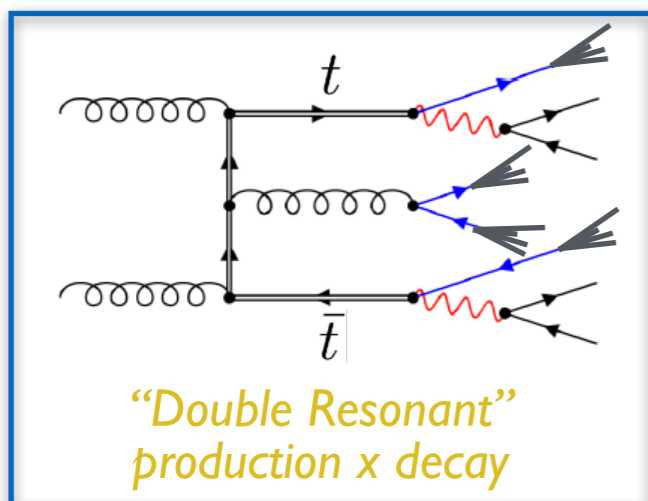


Shower & hadr.

Resonant structures

- Most realistic description of *hadronic observables*
- Based on Narrow Width Approximation for  $t$  and  $W$  decays (with spin correlations)
- Decay matrix elements computed with LO accuracy (radiative effects approximated by PS)

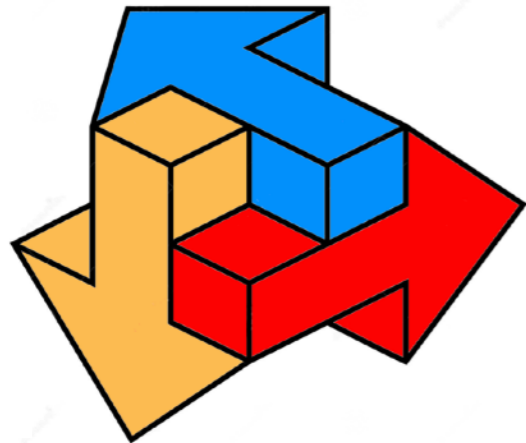
State of the art: **NLO QCD**



- **POWHEG** matching  
Garzelli, Kardos, Trocsanyi '14 '15 [5FS]  
GB, Garzelli, Kardos '17 [4FS]  
Jezo, Lindert, Moretti, Pozzorini '18 [4FS]
- **MC@NLO** matching  
Cascioli, Maierhofer, Moretti, Pozzorini, Siebert '14 [4FS]
- Dedicated comparison of  $t\bar{t}b\bar{b}$  MC's (**LHC HXSWG**)  
Pozzorini, Buccioni, Siebert, Garzelli, GB, Jezo, Krause, Kardos, Lindert, Podskubka, Reuschle and Zaro '21 [4FS]

# Avenues to precision

Higher orders

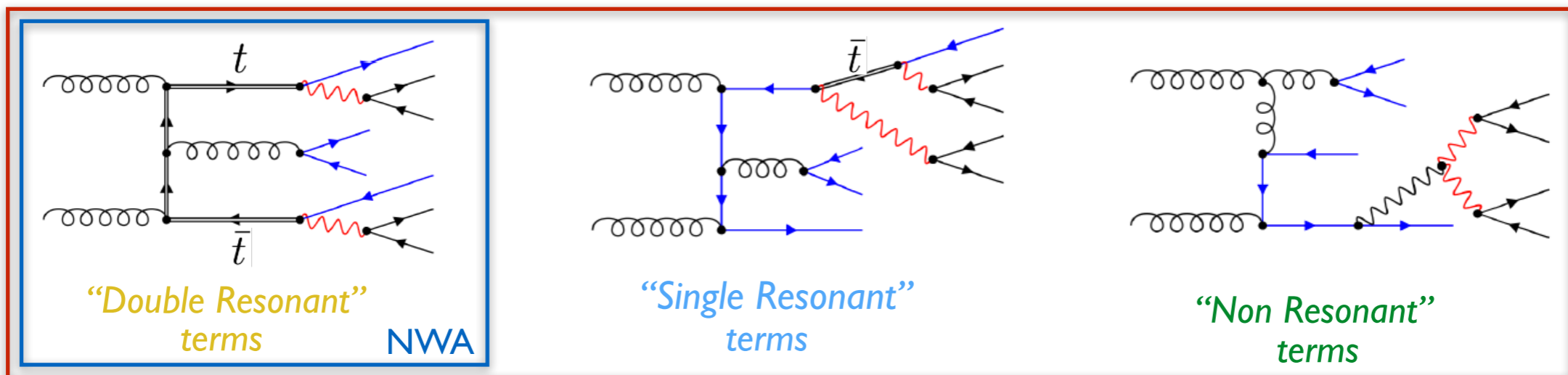


Shower & hadr.

Resonant structures

- Most realistic description of *resonant structures* over phase space
- Drops the limits  $\Gamma_t/m_t \rightarrow 0$ ,  $\Gamma_W/m_W \rightarrow 0$
- Complete calculation of fully decayed process at *fixed order*

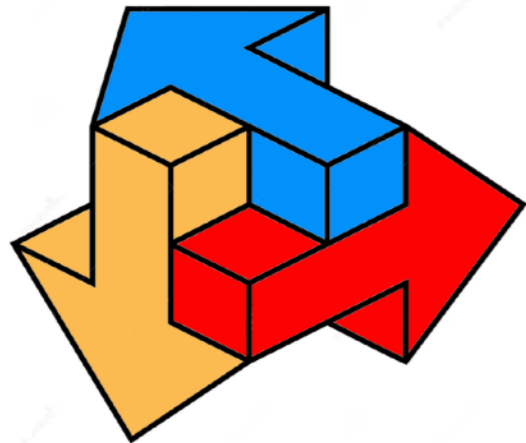
“Off-shell”



$$\text{“Off-shell”} = \text{DR} + \text{SR} + \text{NR} + \text{interferences}$$

# Avenues to precision

Higher orders



Shower & hadr.

Resonant structures

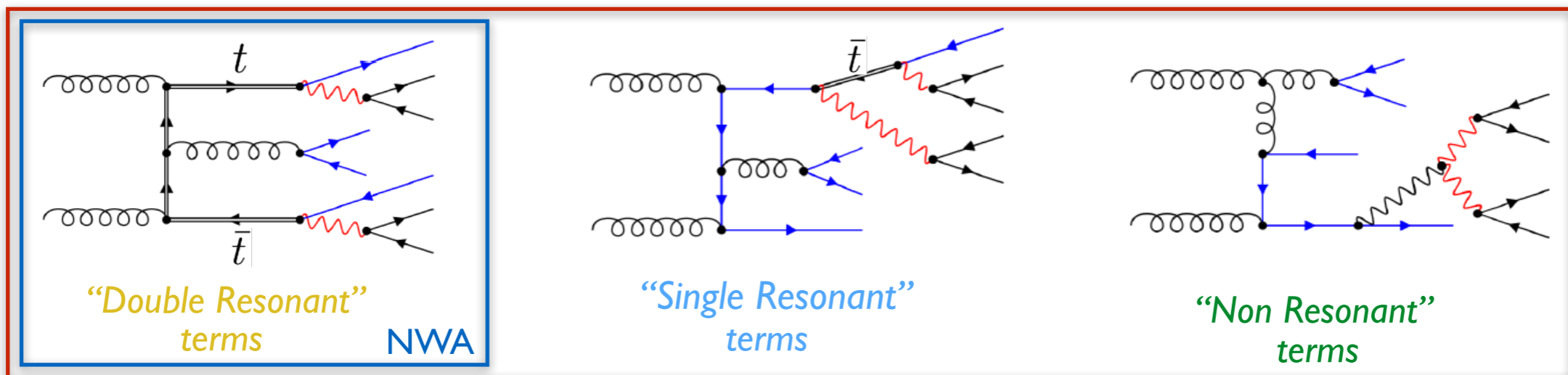
- Most realistic description of resonant structures over phase space
- Drops the limits  $\Gamma_t/m_t \rightarrow 0$ ,  $\Gamma_W/m_W \rightarrow 0$
- Complete calculation of fully decayed process at fixed order

Focus of this talk

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b}$$

Denner, Lang, Pellen '21

GB, Bi, Hartanto, Kraus, Lupattelli, Worek '21 '23



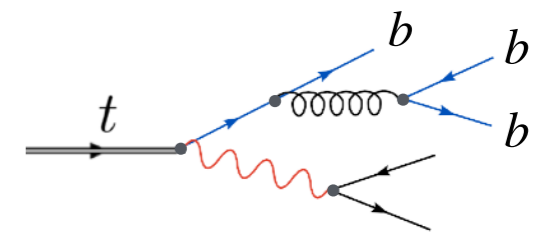
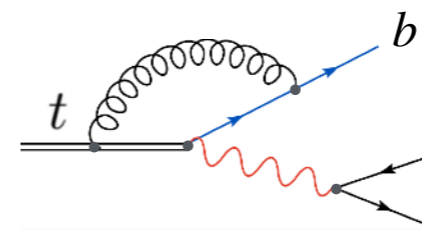
$$\text{“Off-shell”} = \text{DR} + \text{SR} + \text{NR} + \text{interferences}$$

# Topics covered in this talk

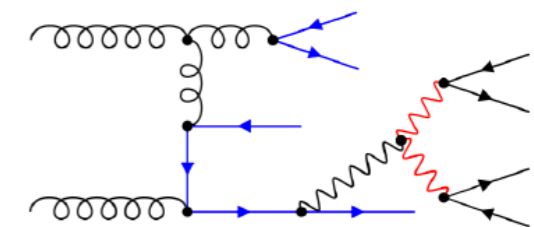
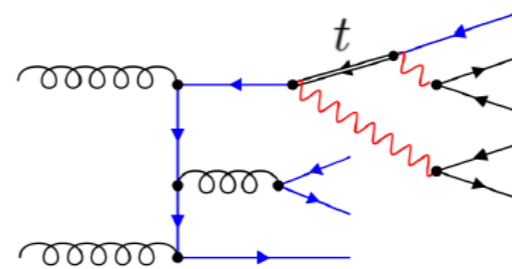
- Dominant **theory uncertainties** in  $t\bar{t}b\bar{b}$  with *dilepton* signatures

- Impact of top-quark **decay modelling accuracy**

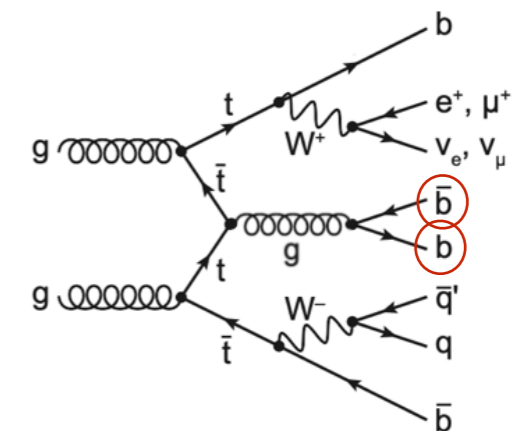
- QCD corrections to top decays
- Multi  $b$ -jet top decays



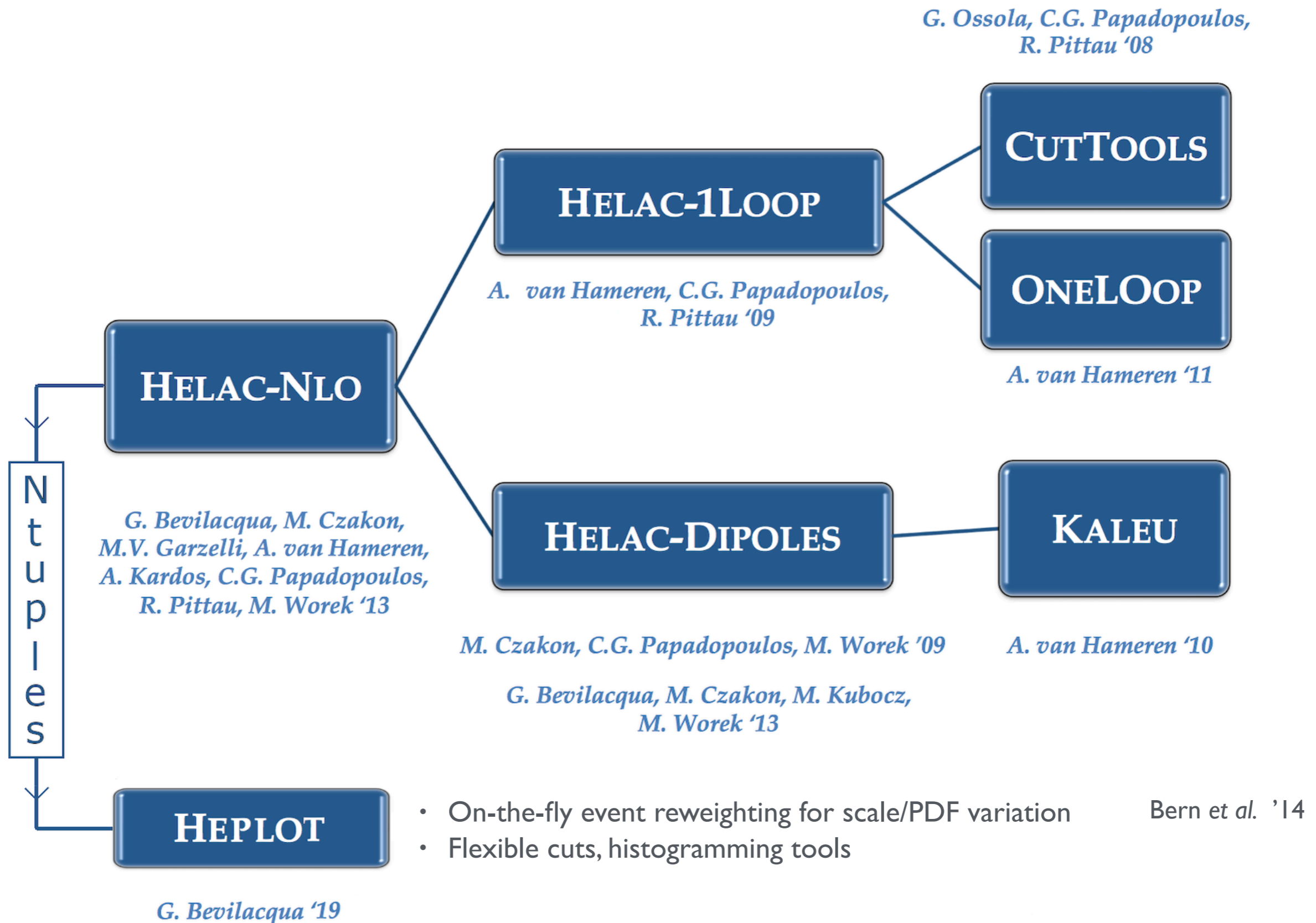
- Impact of **full off-shell effects** for  $t$  and  $W$  decays



- $b$ -jet labelling and **identification of prompt  $b$ -jets**



# Computational framework

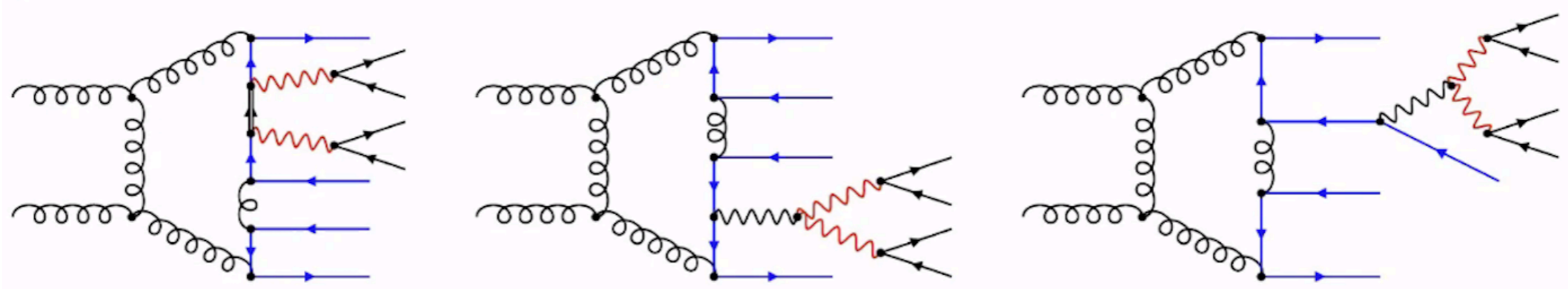


# Technical aspects of off-shell $t\bar{t}b\bar{b}$ at NLO

One-loop correction type	Number of Feynman diagrams
Self-energy	93452
Vertex	88164
Box-type	49000
Pentagon-type	25876
Hexagon-type	11372
Heptagon-type	3328
Octagon-type	336
<b>Total number [gg channel]</b>	<b>271528</b>

$$gg \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b}$$

Partonic Subprocess	Number of Feynman diagrams	Number of CS Dipoles	Number of NS Subtractions
$gg \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} g$	41364	90	18
$q\bar{q} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} g$	9576	50	10
$gq \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} q$	9576	50	10
$g\bar{q} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} \bar{q}$	9576	50	10



# I. Size of QCD corrections and dominant theory uncertainties at NLO

# $t\bar{t}b\bar{b}$ with dilepton signatures: full off-shell predictions

- Integrated fiducial cross sections

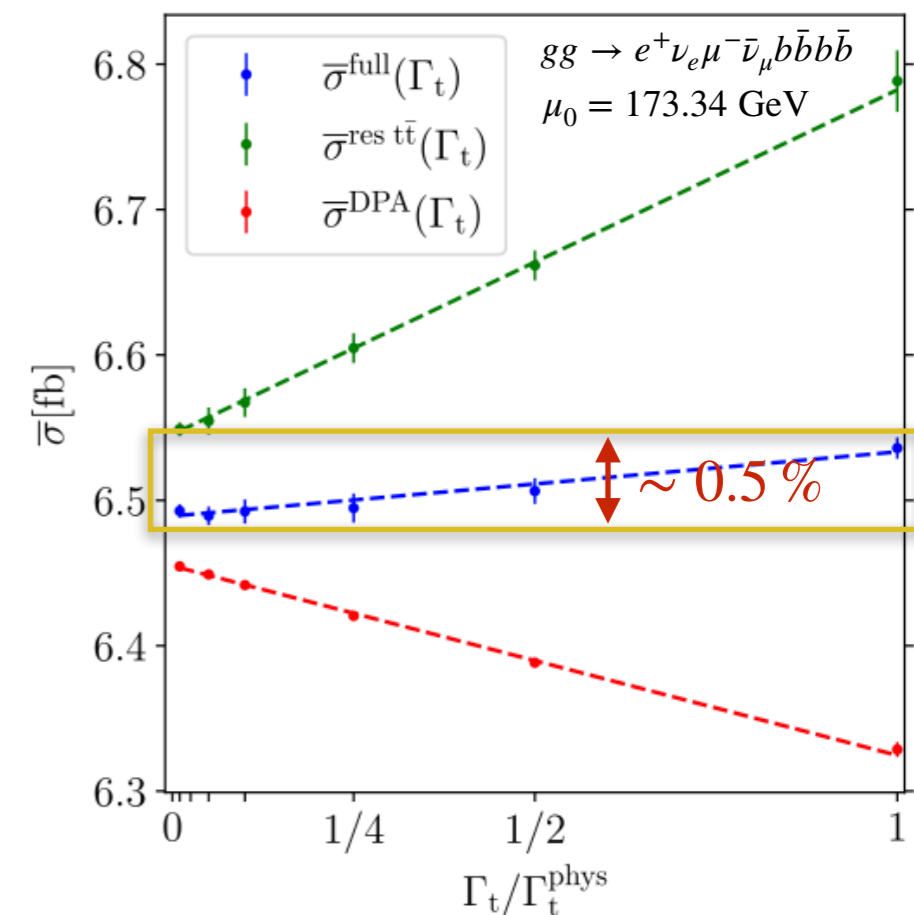
$$\sqrt{s} = 13 \text{ TeV}$$

Analysis cuts:  $p_T(\ell) > 20 \text{ GeV}$ ,  $p_T(b) > 25 \text{ GeV}$ ,  $|y(\ell)| < 2.5$ ,  $|y(b)| < 2.5$

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [JHEP 08 \(2021\) 008](#)]

$p_T(b)$	$\sigma^{\text{LO}}$ [fb]	$\delta_{\text{scale}}$	$\sigma^{\text{NLO}}$ [fb]	$\delta_{\text{scale}}$	$\delta_{\text{PDF}}$	$\mathcal{K} = \sigma^{\text{NLO}}/\sigma^{\text{LO}}$
$\mu_R = \mu_F = \mu_0 = H_T/3$ [NNPDF 3.1]						
25	6.813	+4.338 (64%) -2.481 (36%)	13.22	+2.66 (20%) -2.95 (22%)	+0.19 (1%) -0.19 (1%)	1.94
30	4.809	+3.062 (64%) -1.756 (37%)	9.09	+1.66 (18%) -1.98 (22%)	+0.16 (2%) -0.16 (2%)	1.89
35	3.431	+2.191 (64%) -1.256 (37%)	6.37	+1.07 (17%) -1.36 (21%)	+0.11 (2%) -0.11 (2%)	1.86
40	2.464	+1.582 (64%) -0.901 (37%)	4.51	+0.72 (16%) -0.95 (21%)	+0.09 (2%) -0.09 (2%)	1.83

[Denner, Lang, Pellen, [Phys. Rev. D 104 \(2021\), 056018](#)]



- QCD corrections are large

- Impact of jet veto:

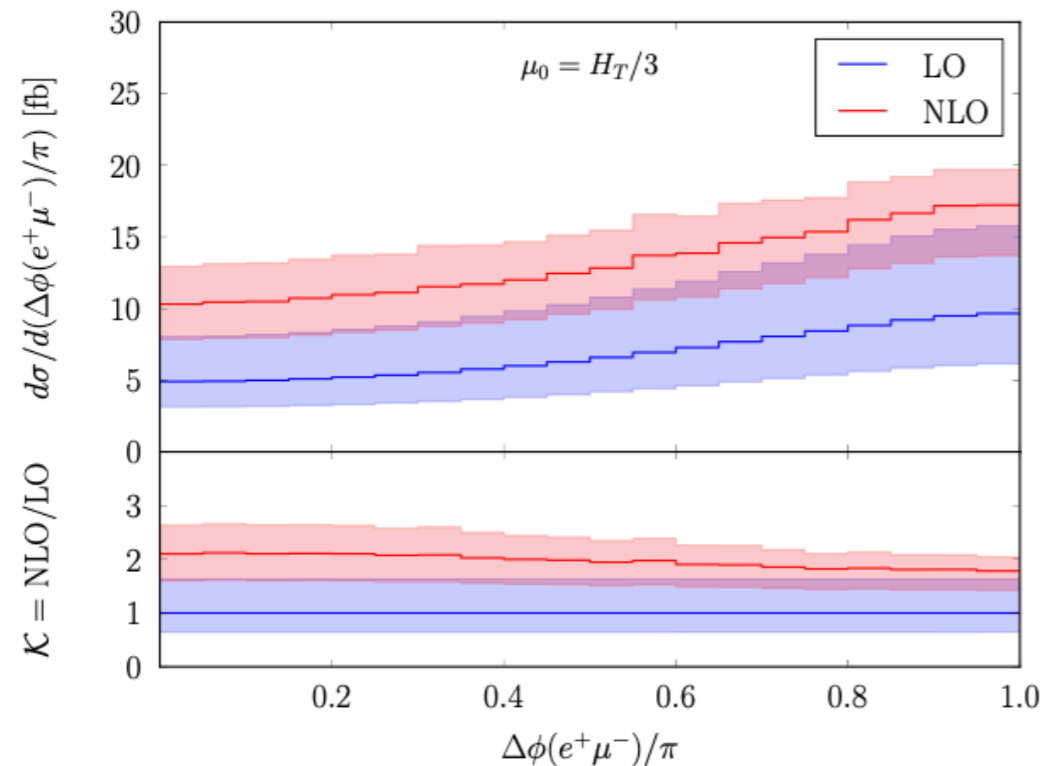
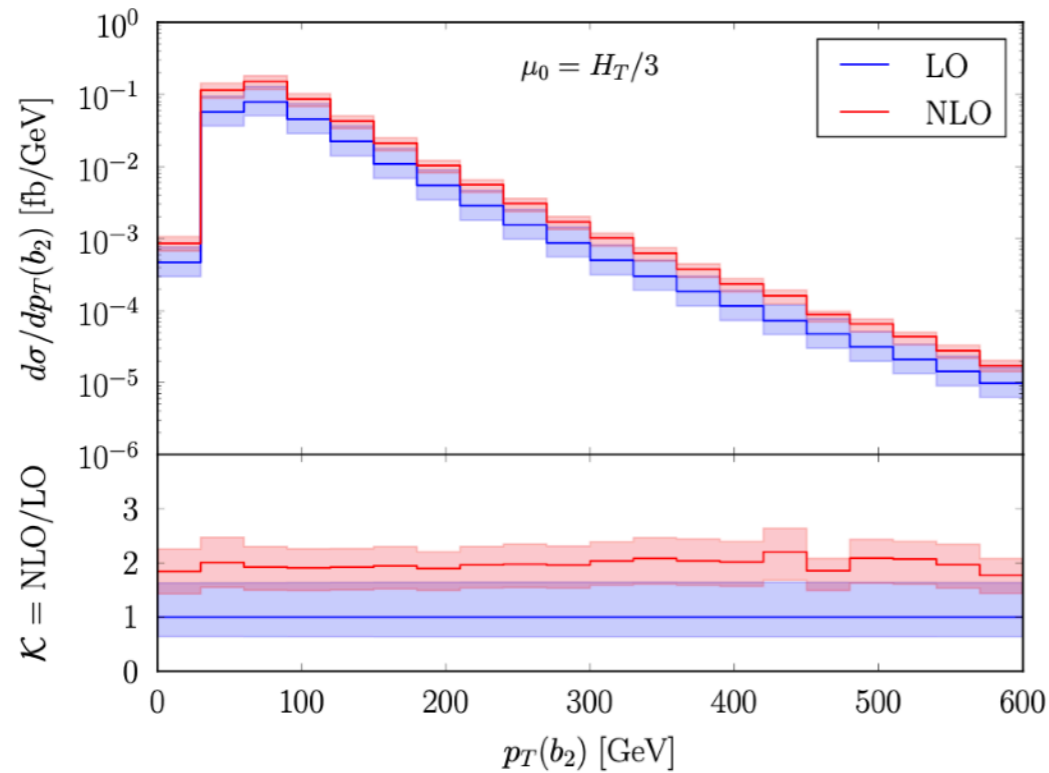
$$p_T^{\text{veto}}(j) = 100 \text{ GeV} \rightarrow \sigma^{\text{NLO}}/\sigma^{\text{LO}} = 1.58$$

$$p_T^{\text{veto}}(j) = 50 \text{ GeV} \rightarrow \sigma^{\text{NLO}}/\sigma^{\text{LO}} = 1.23$$

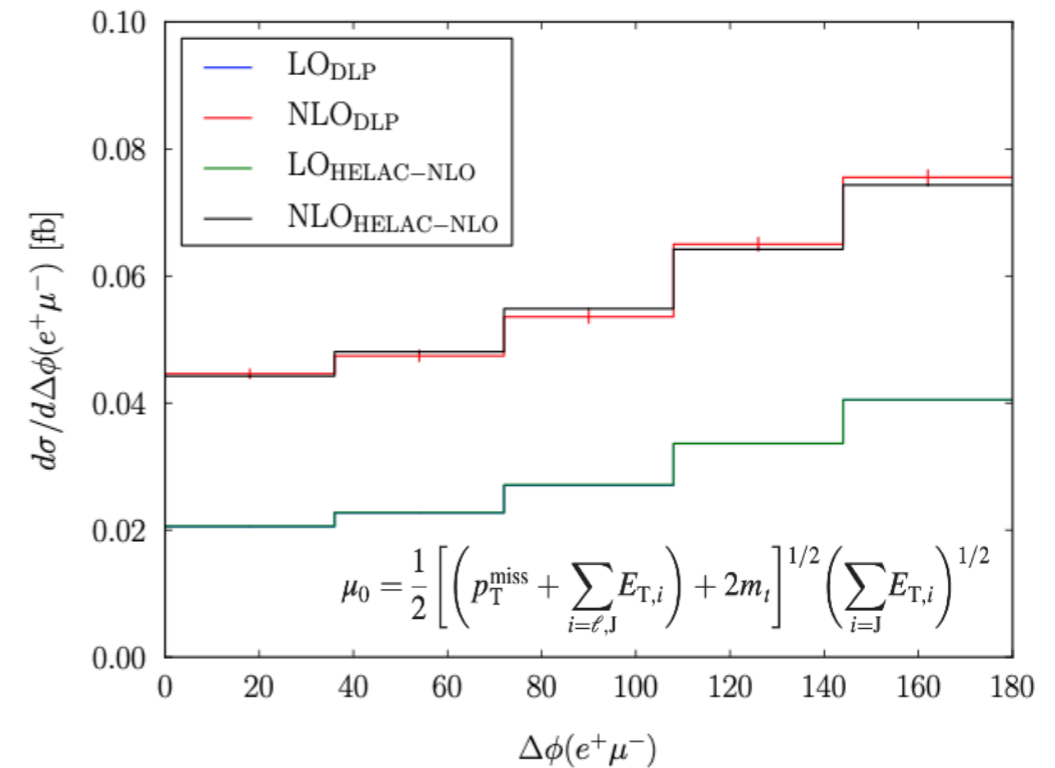
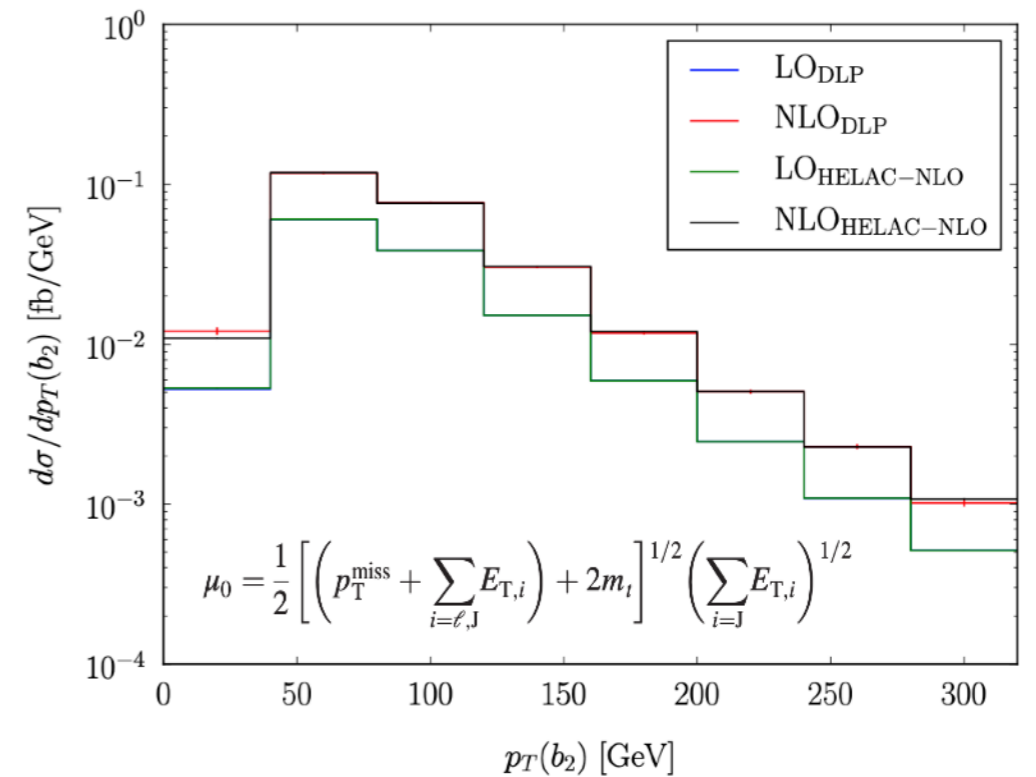


# Off-shell $t\bar{t}b\bar{b}$ : differential cross sections

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek,  
[JHEP 08 \(2021\) 008](#)]

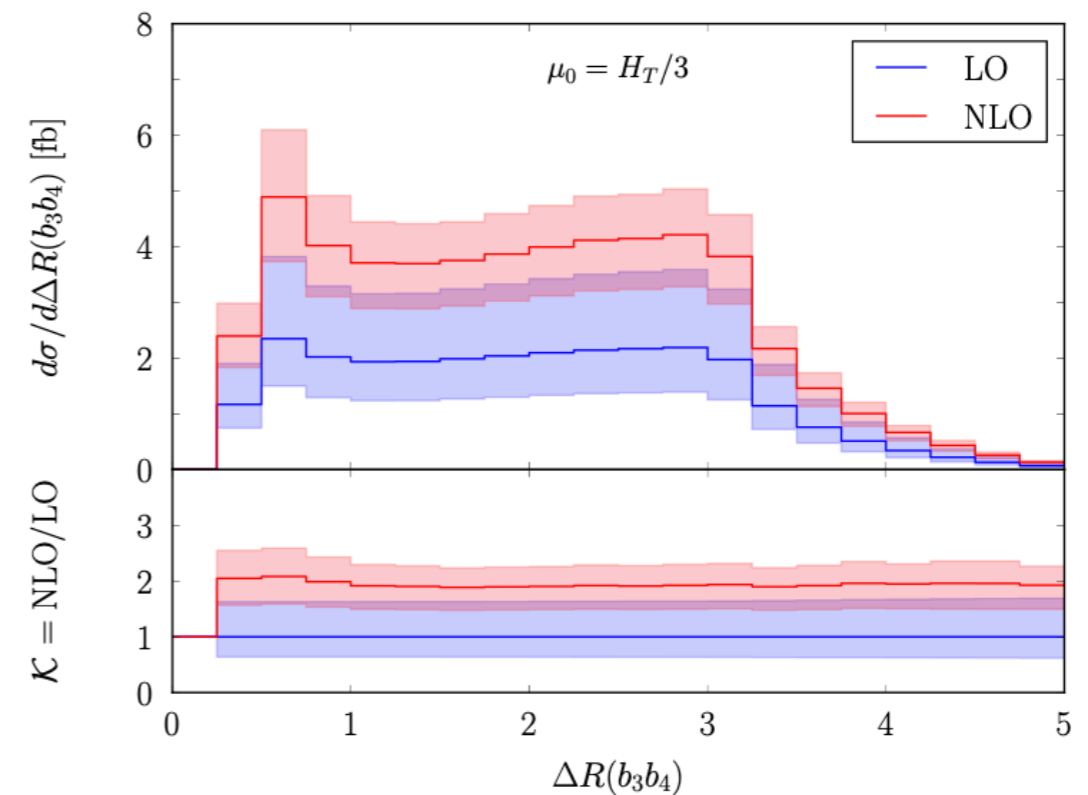
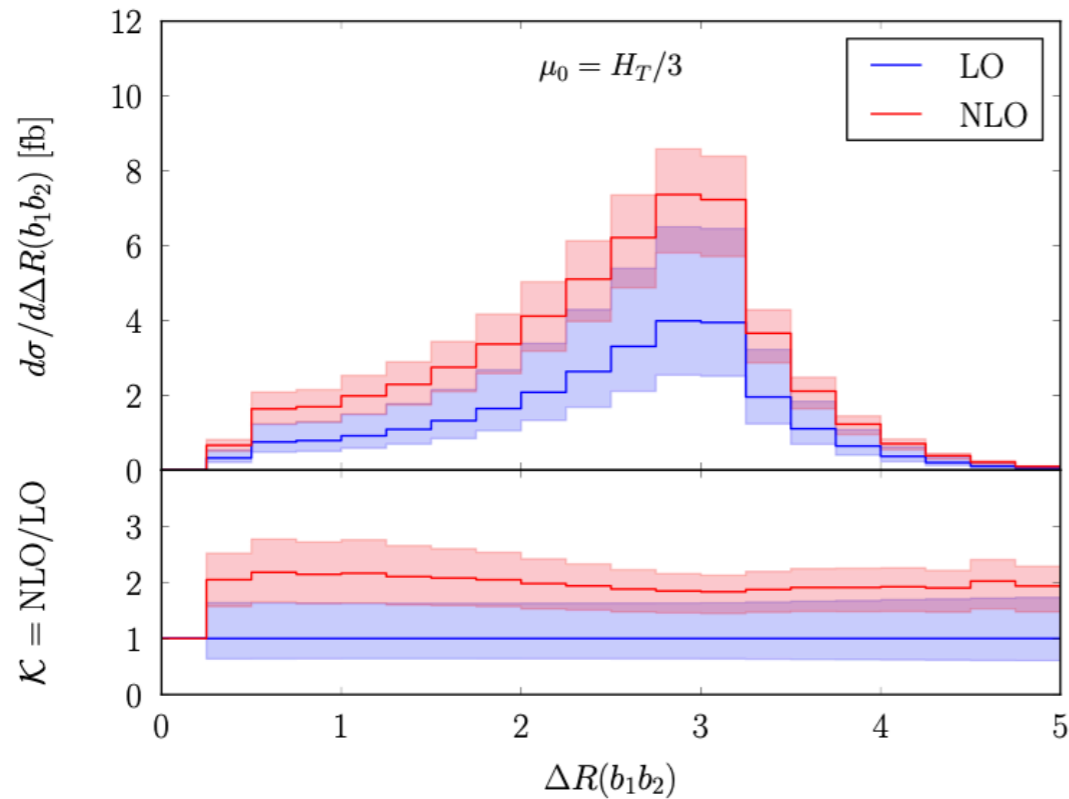
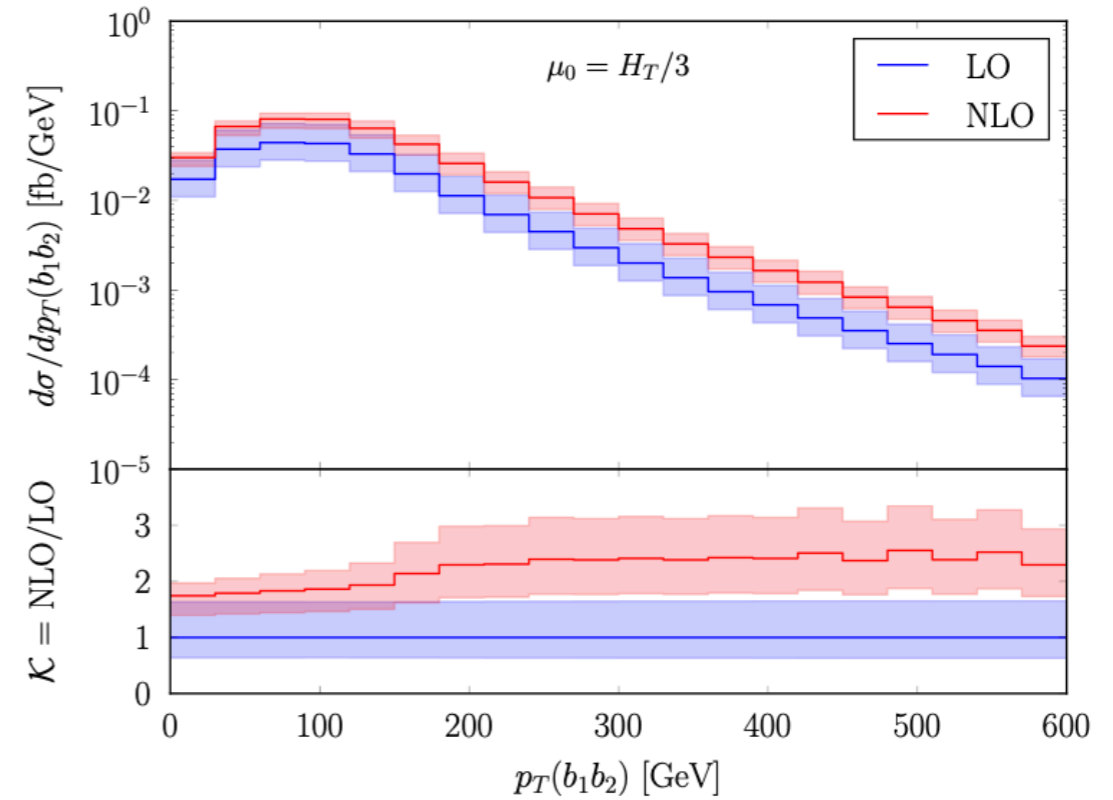
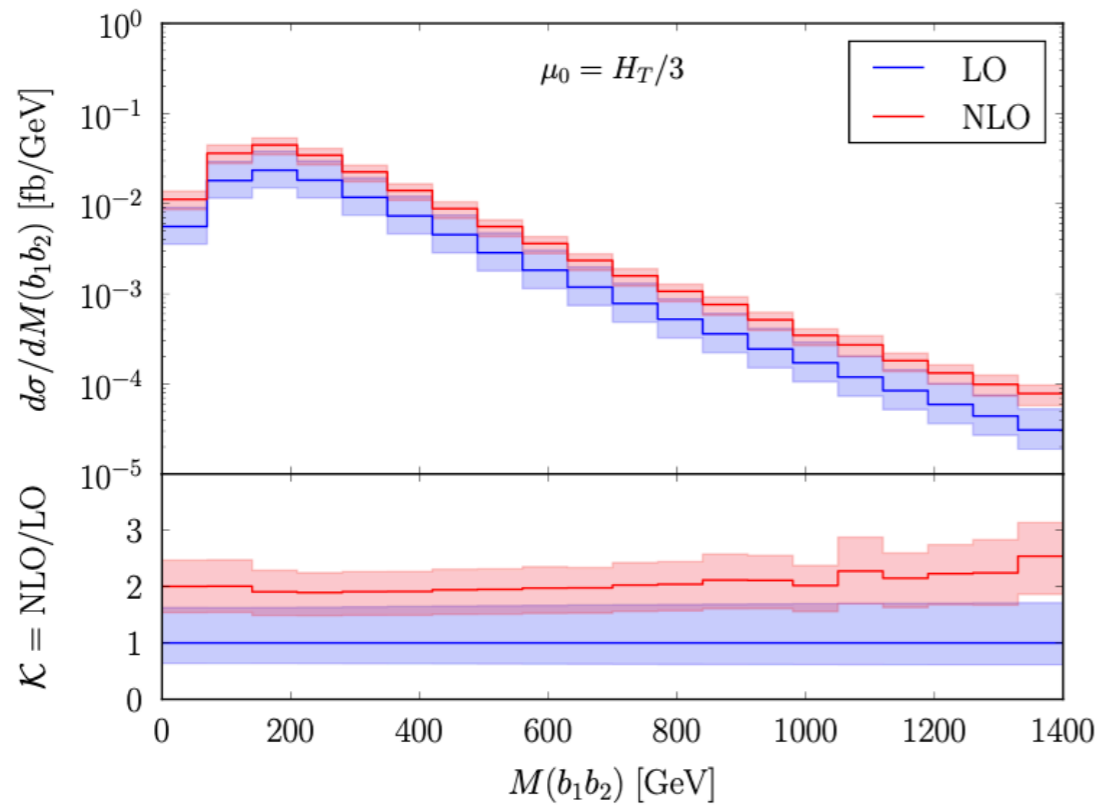


Comparison with Denner, Lang and Pellen,  
[\[Phys. Rev. D 104 \(2021\), 056018\]](#)



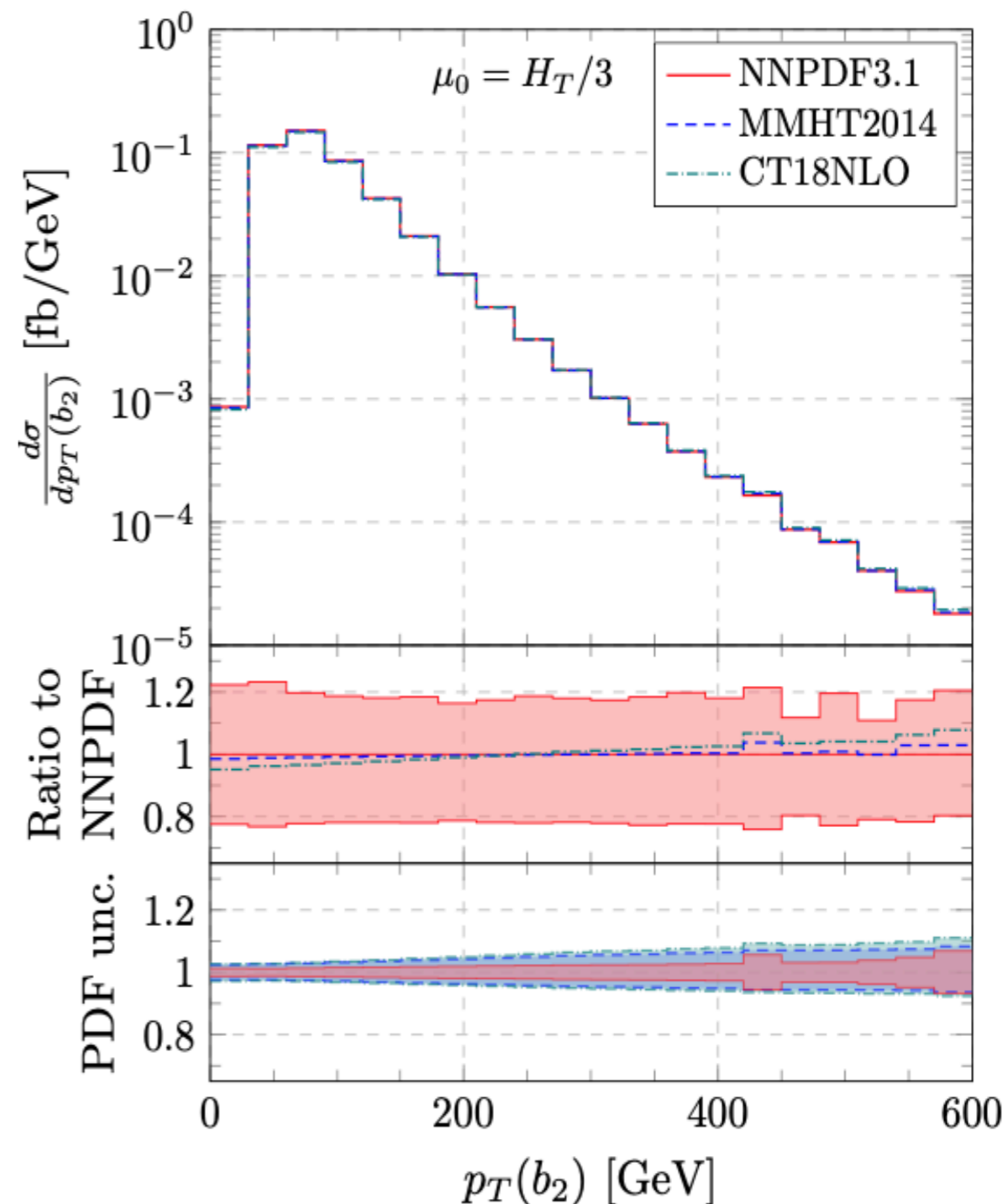
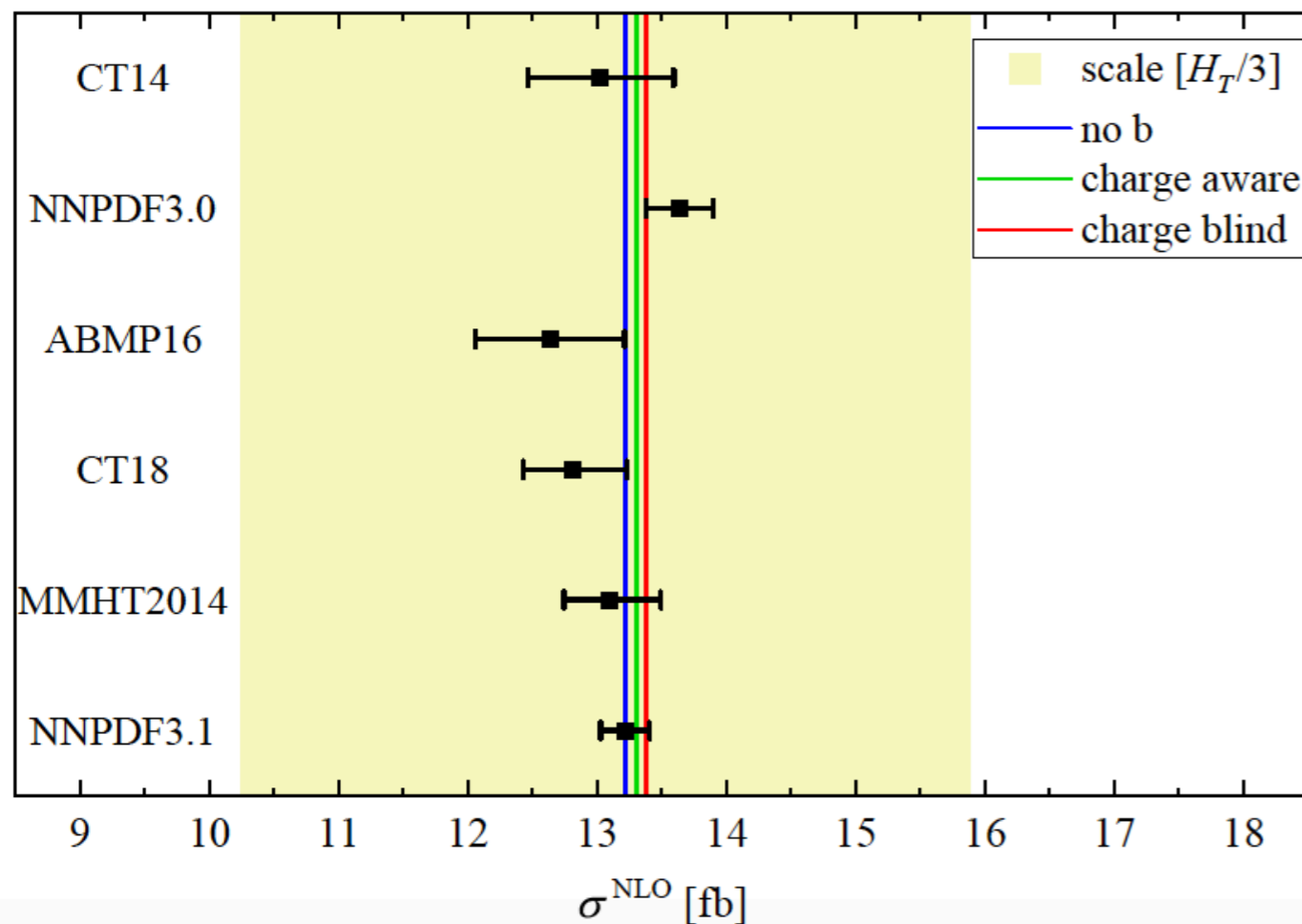
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[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [JHEP 08 \(2021\) 008](#)]



# Off-shell $t\bar{t}b\bar{b}$ : theoretical uncertainties at NLO

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [JHEP 08 \(2021\) 008](#)]



## NLO theory uncertainties

- Scale :  $\mathcal{O}(20\%)$  - PDF :  $\mathcal{O}(1\% - 3\%)$

↪ Relative sizes vary at high-energy tails

## II. Accuracy of NWA and off-shell effects

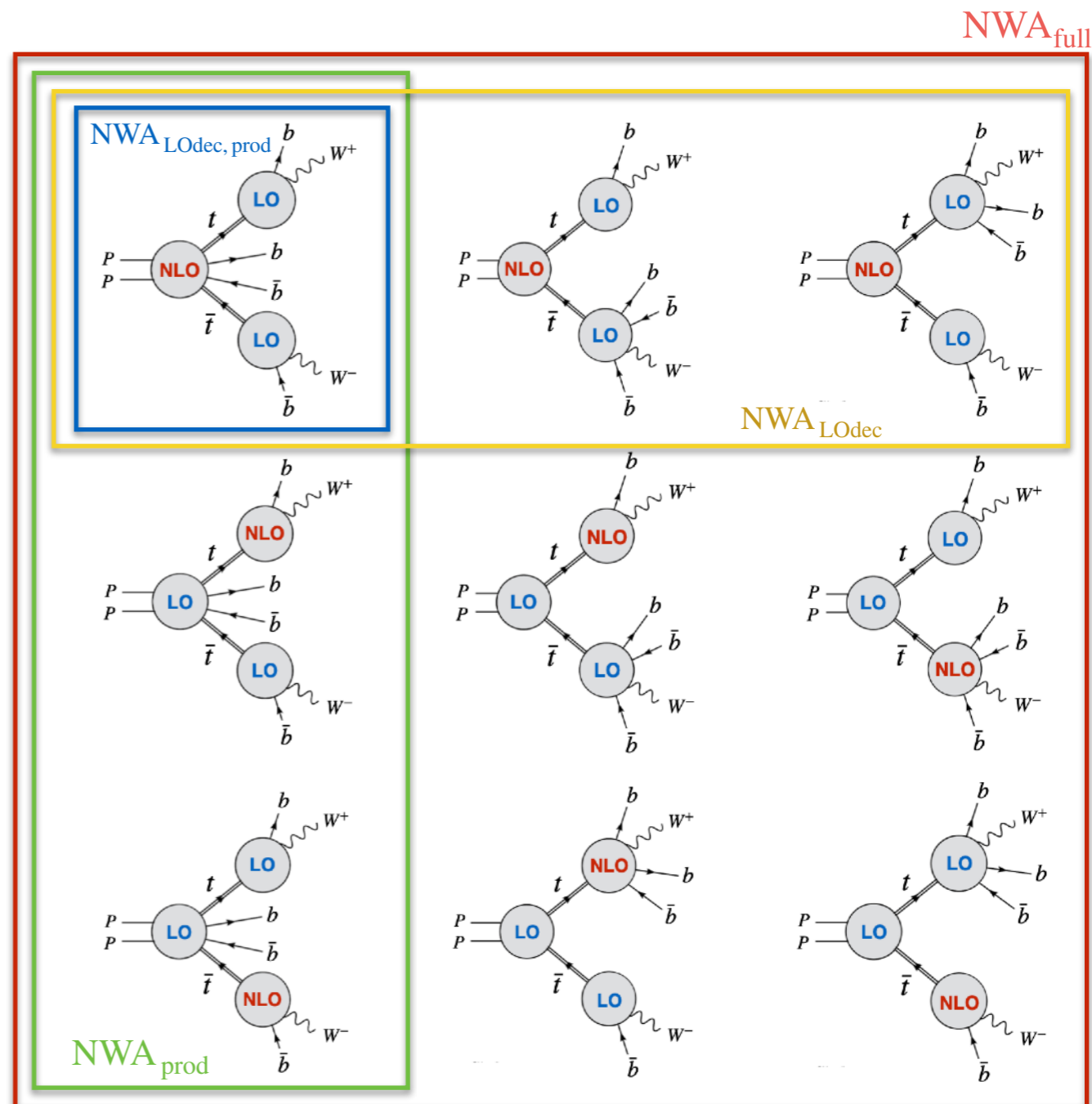
# $t\bar{t}b\bar{b}$ : comparing modelling approaches

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [Phys. Rev. D \(107\) 2023](#)]

- Full off-shell vs NWA

Modelling	$\sigma^{\text{NLO}}$ [fb]	$\delta_{\text{scale}}$ [fb]	$\frac{\sigma^{\text{NLO}}}{\sigma^{\text{NWA}_{\text{full}}}} - 1$
Off-shell	13.22(2)	+2.65 (20%) -2.96 (22%)	+0.5%
<b>NWA<sub>full</sub></b>	<b>13.16(1)</b>	<b>+2.61 (20%) -2.93 (22%)</b>	—
NWA <sub>LOdec</sub>	13.22(1)	+3.77 (29%) -3.31 (25%)	+0.5%
NWA <sub>prod</sub>	13.01(1)	+2.58 (20%) -2.89 (22%)	-1.1%
NWA <sub>prod, exp</sub>	12.25(1)	+2.87 (23%) -2.86 (23%)	-6.9%
<b>NWA<sub>prod, LOdec</sub></b>	<b>13.11(1)</b>	<b>+3.74 (29%) -3.28 (25%)</b>	-0.4%

- NWA cross sections based on different levels of accuracy in top decay modelling



# $t\bar{t}b\bar{b}$ : comparing modelling approaches

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [Phys. Rev. D \(107\) 2023](#)]

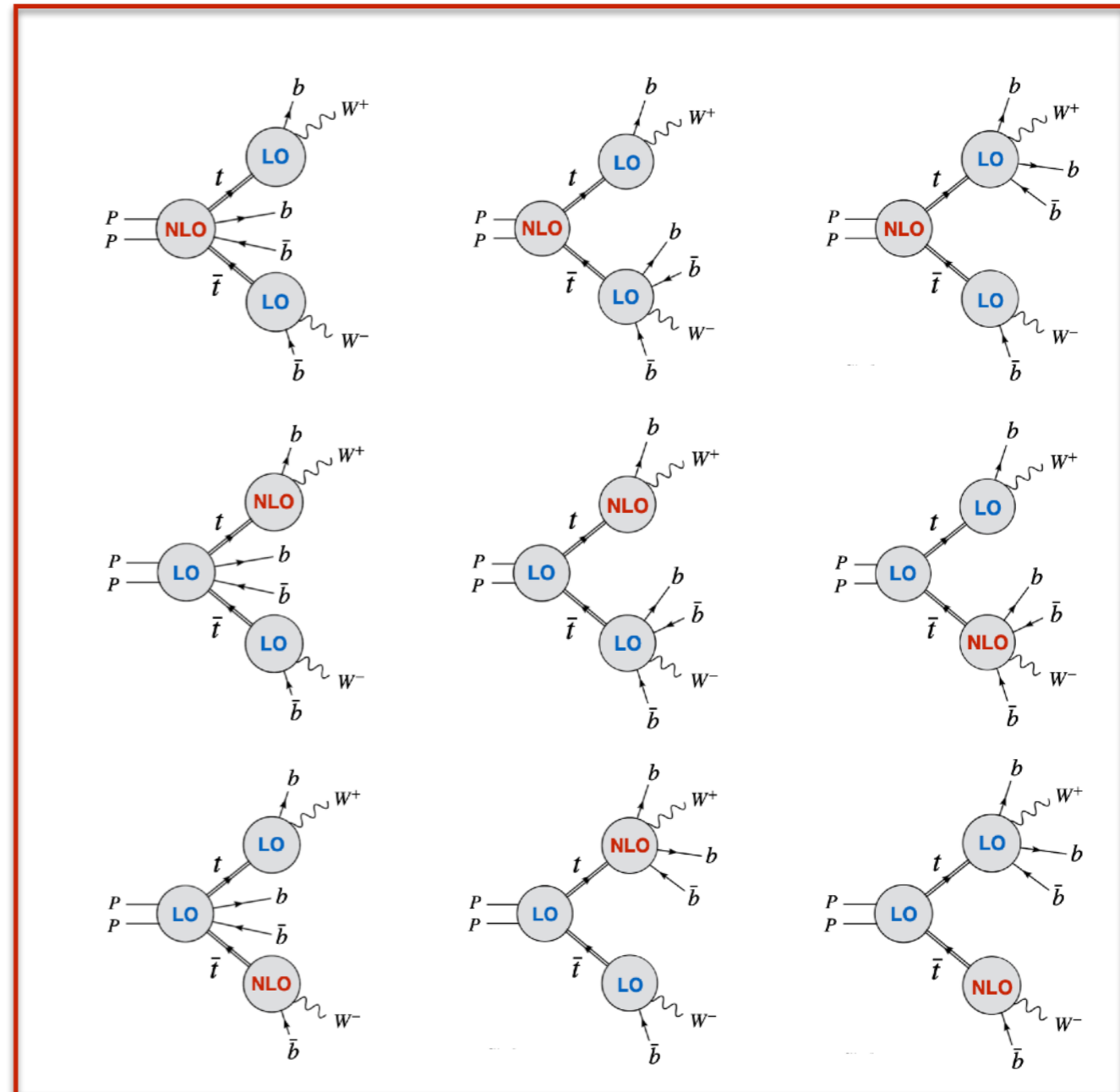
- Full off-shell vs NWA

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- Off-shell vs NWA<sub>full</sub>:

↪ Off-shell effects: +0.5%

NWA<sub>full</sub>



# $t\bar{t}b\bar{b}$ : comparing modelling approaches

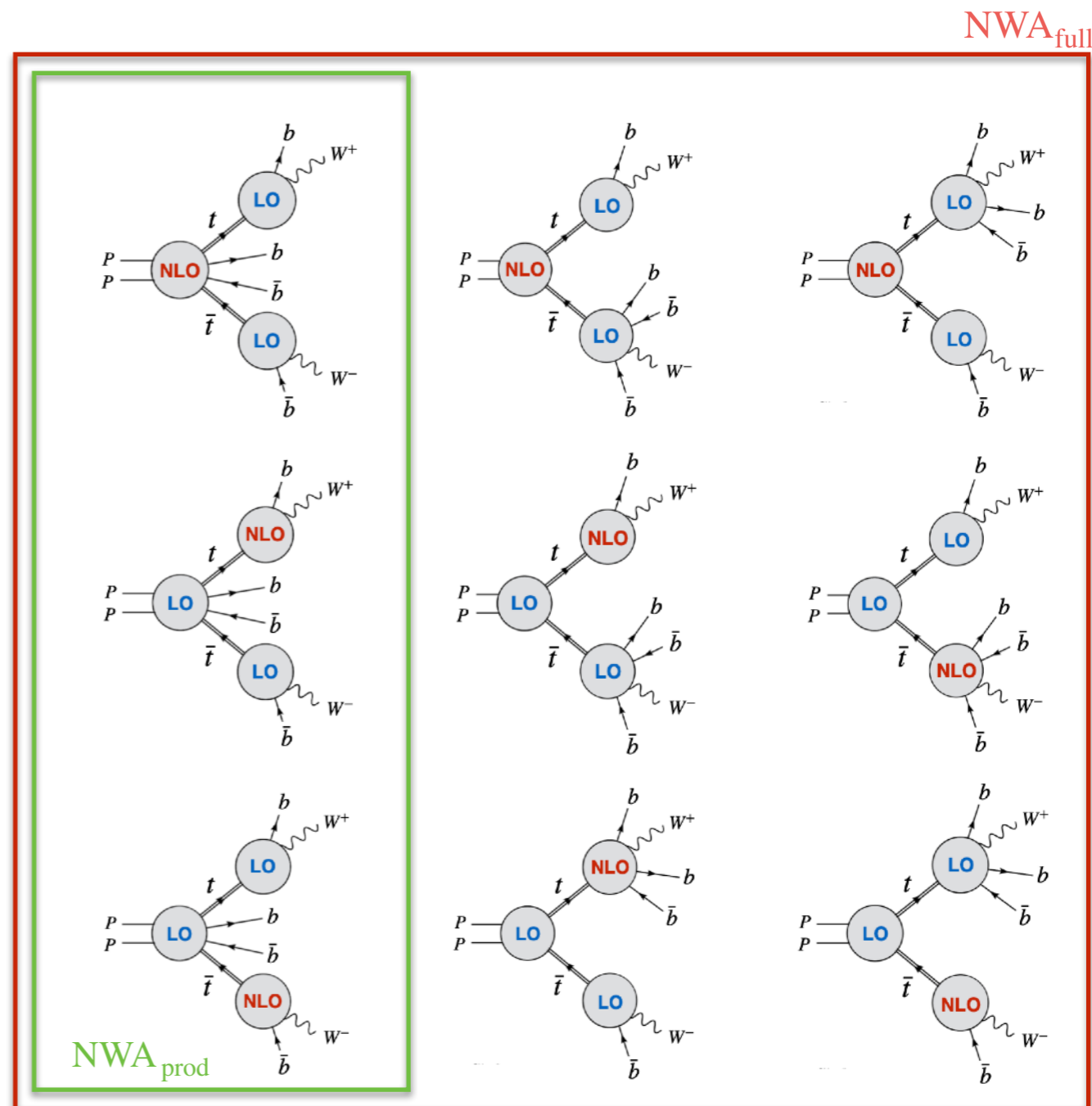
[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [Phys. Rev. D \(107\) 2023](#)]

- Full off-shell vs NWA

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NWA <sub>prod, LOdec</sub>	13.11(1)	+3.74 (29%) -3.28 (25%)	-0.4%

- NWA<sub>full</sub> vs NWA<sub>prod</sub> :

↪ Impact of  $t \rightarrow Wb\bar{b}$  decays: +1%



# $t\bar{t}b\bar{b}$ : comparing modelling approaches

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [Phys. Rev. D \(107\) 2023](#)]

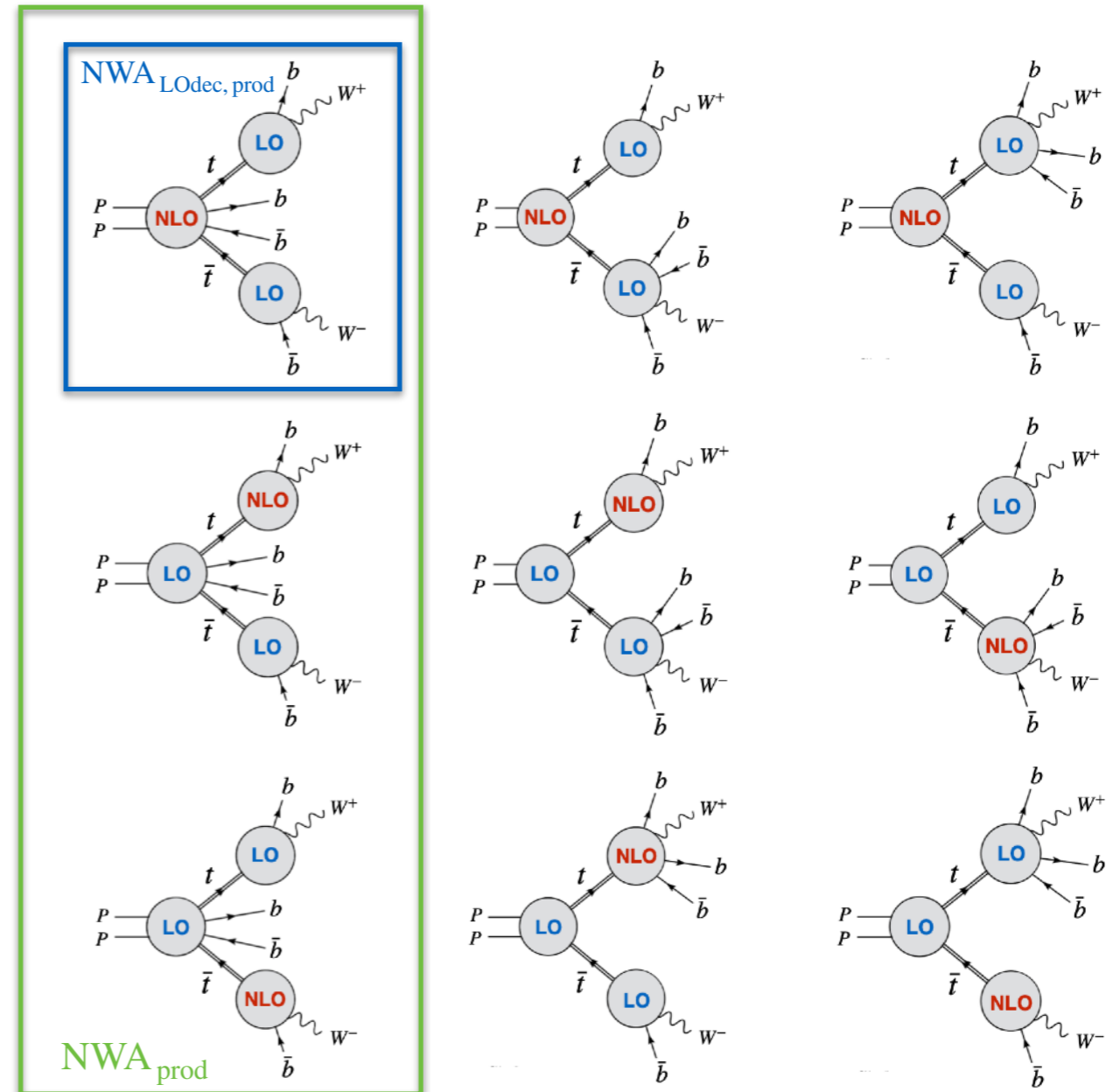
- Full off-shell vs NWA

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- NWA<sub>prod</sub> vs NWA<sub>prod,LOdec</sub> :

↪ Tiny difference: 0.8%

How shall this be interpreted?





# $t\bar{t}b\bar{b}$ : comparing modelling approaches

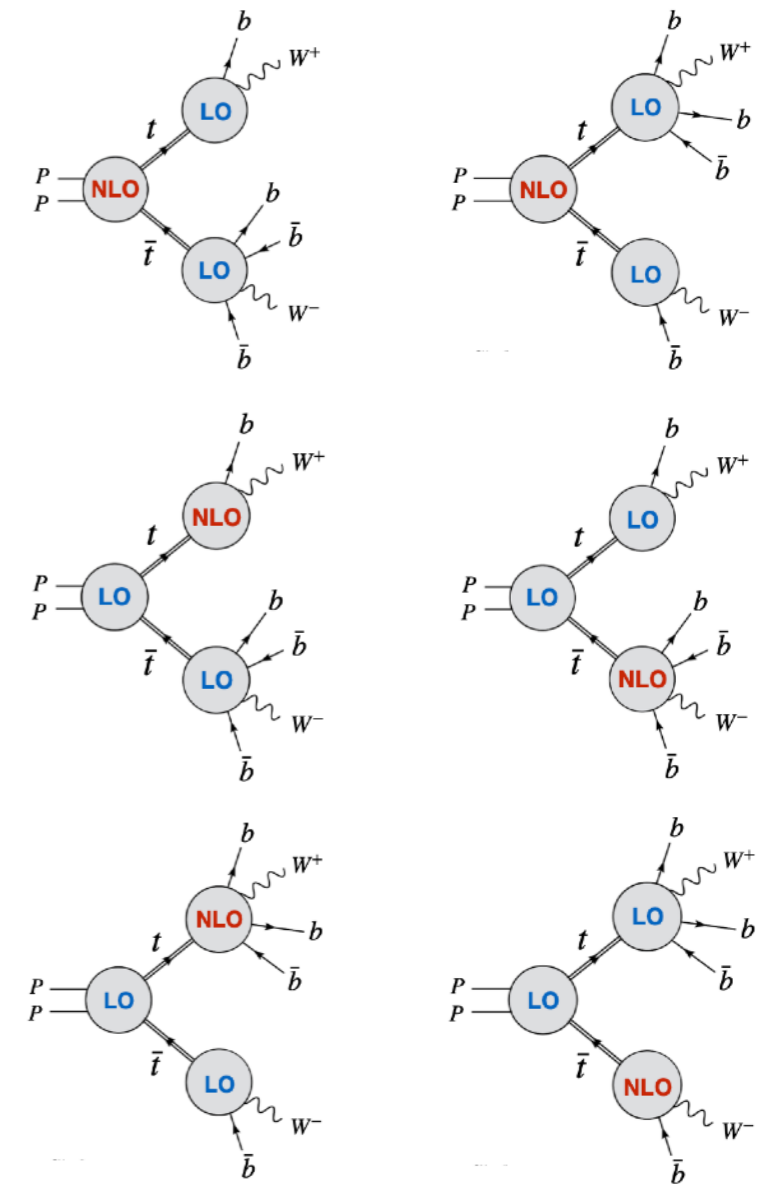
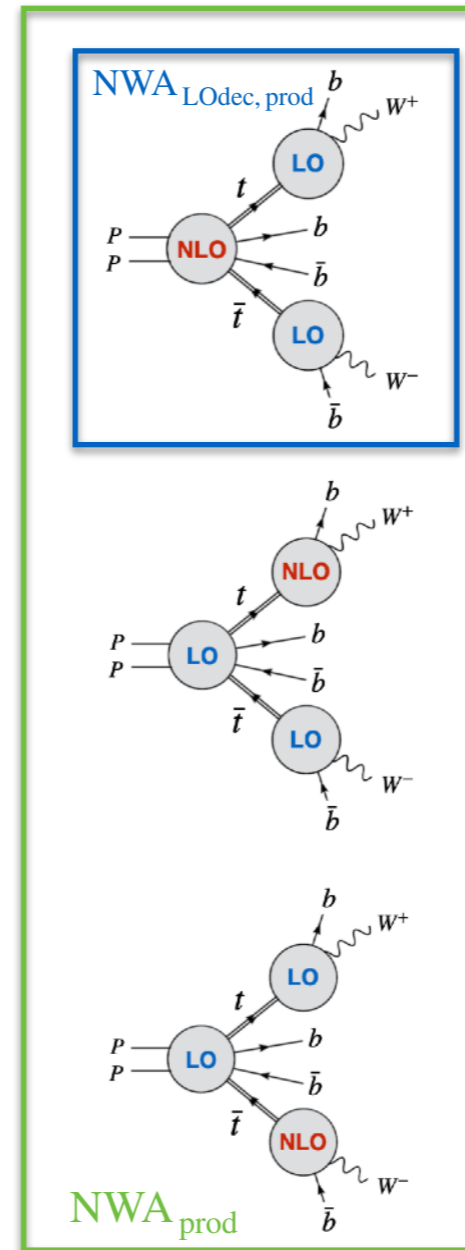
[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [Phys. Rev. D \(107\) 2023](#)]

- Full off-shell vs NWA

Modelling	$\sigma^{\text{NLO}}$ [fb]	$\delta_{\text{scale}}$ [fb]	$\frac{\sigma^{\text{NLO}}}{\sigma^{\text{NWA}_{\text{full}}}} - 1$
Off-shell	13.22(2)	+2.65 (20%) -2.96 (22%)	+0.5%
NWA <sub>full</sub>	13.16(1)	+2.61 (20%) -2.93 (22%)	—
NWA <sub>LOdec</sub>	13.22(1)	+3.77 (29%) -3.31 (25%)	+0.5%
NWA <sub>prod</sub>	13.01(1)	+2.58 (20%) -2.89 (22%)	-1.1%
NWA <sub>prod,exp</sub>	12.25(1)	+2.87 (23%) -2.86 (23%)	-6.9%
NWA <sub>prod,LOdec</sub>	13.11(1)	+3.74 (29%) -3.28 (25%)	-0.4%

- NWA<sub>prod,exp</sub> vs NWA<sub>prod,LOdec</sub> :

↪ Genuine QCD corrections to top decays: -7%



# $t\bar{t}b\bar{b}$ : comparing modelling approaches

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [Phys. Rev. D \(107\) 2023](#)]

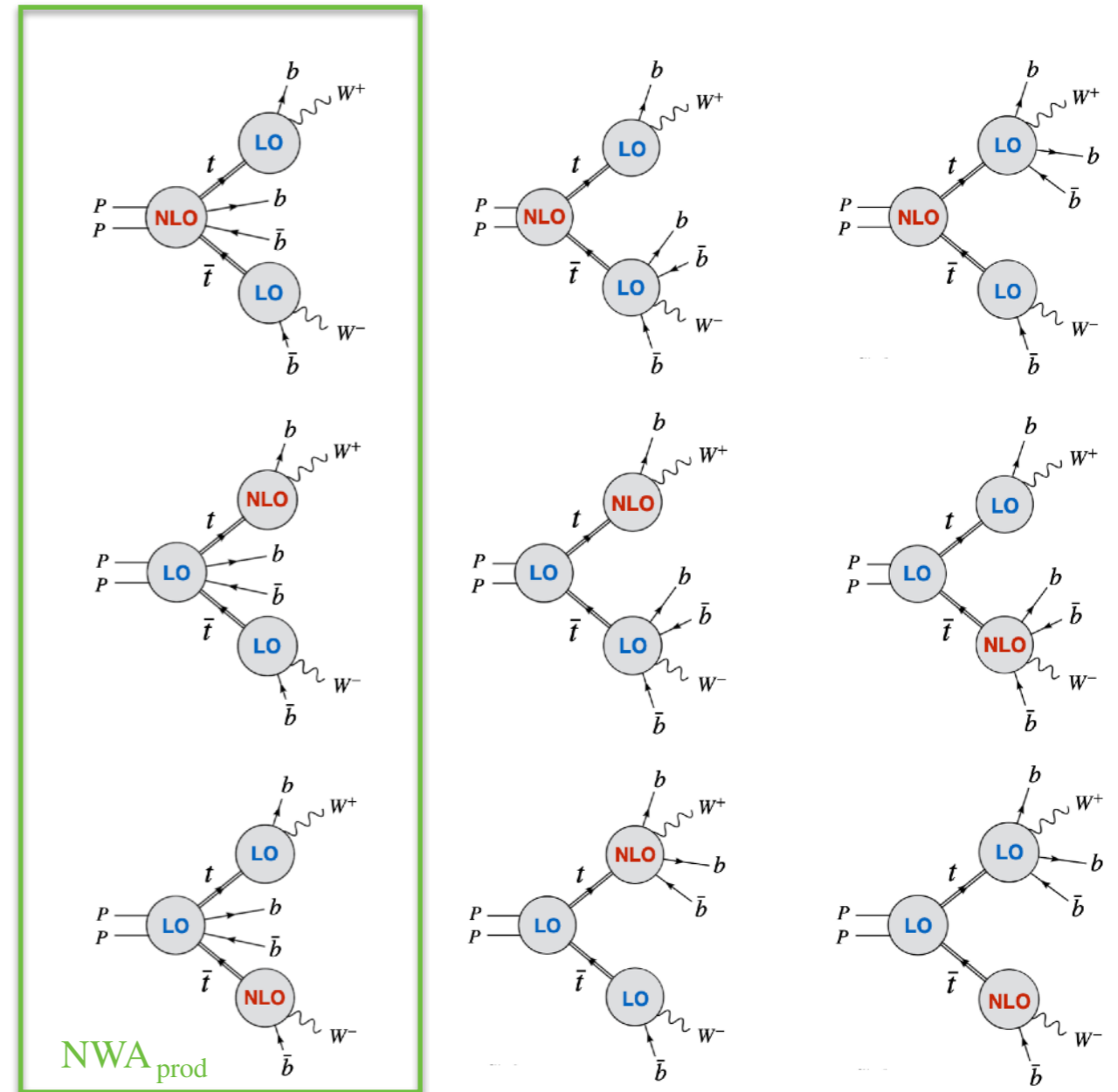
## • Full off-shell vs NWA

Modelling	$\sigma^{\text{NLO}}$ [fb]	$\delta_{\text{scale}}$ [fb]	$\frac{\sigma^{\text{NLO}}}{\sigma^{\text{NWA}_{\text{full}}}} - 1$
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NWA <sub>prod,LOdec</sub>	13.11(1)	+3.74 (29%) -3.28 (25%)	-0.4%

• NWA<sub>prod</sub> vs NWA<sub>prod,exp</sub> :

↪ Impact of  $\Gamma_t^{\text{NLO}}$  expansion: +6%

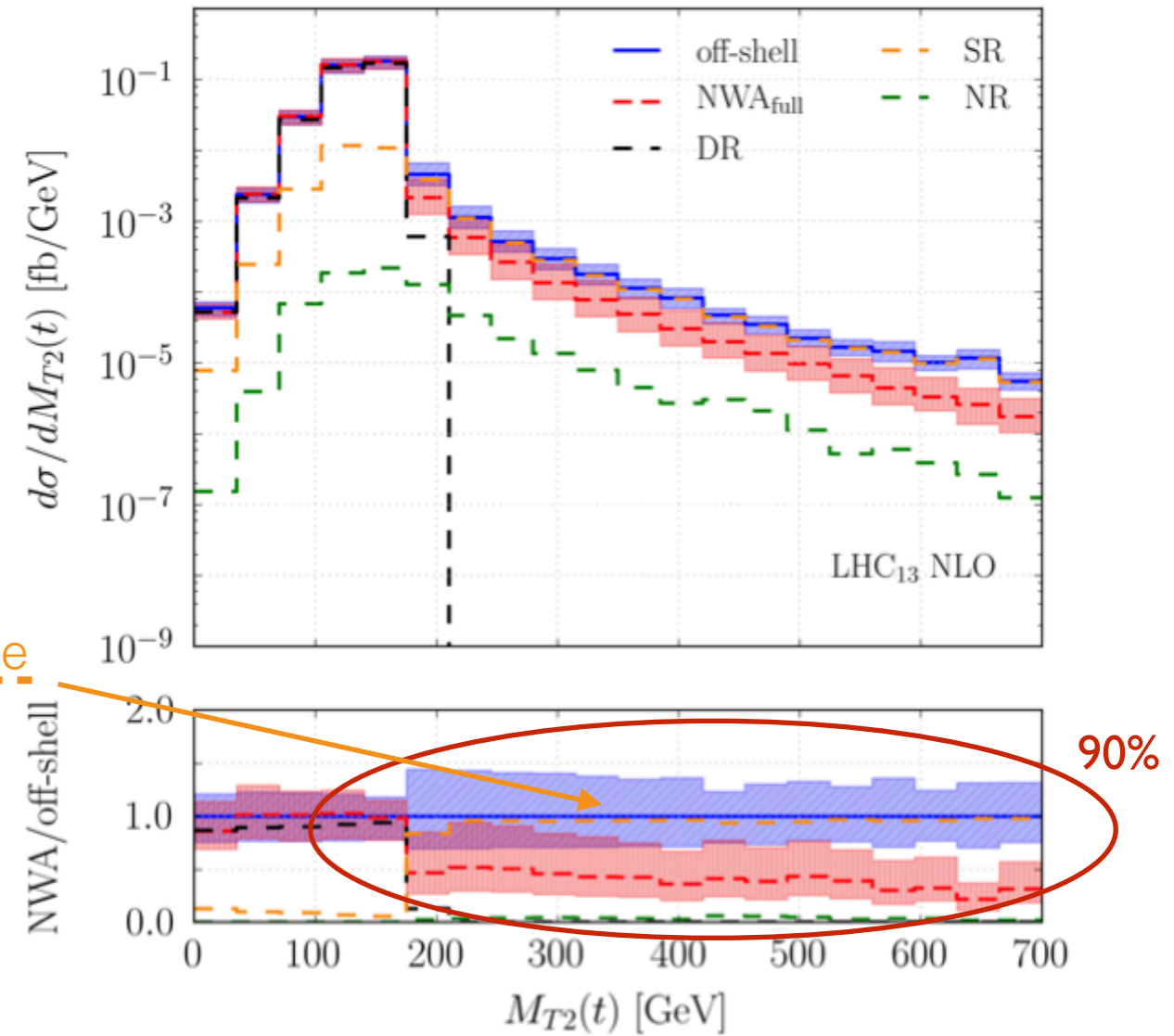
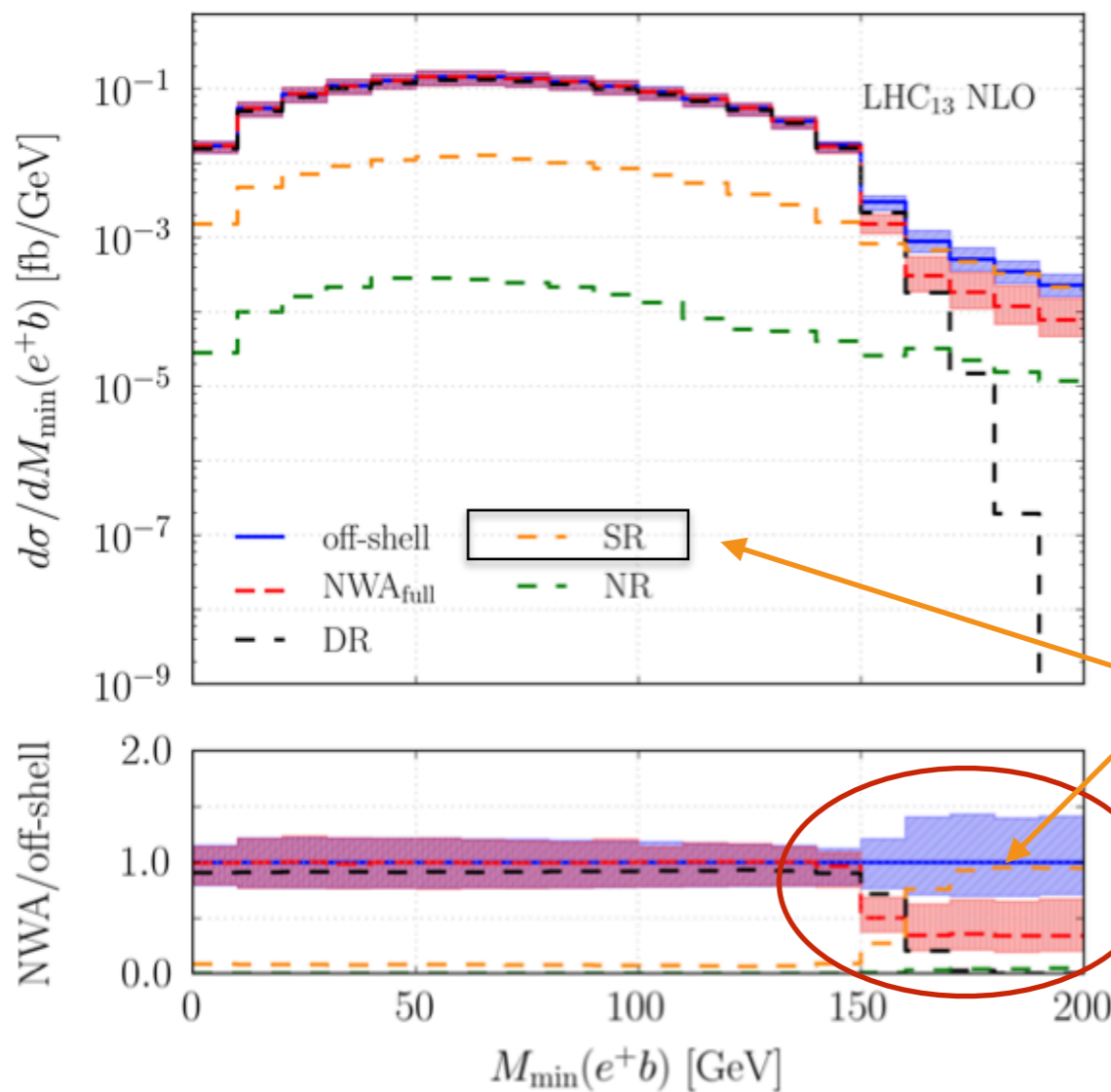
$\mathcal{O}(\alpha_s^2)$  effects (within NLO scale uncertainty)



# $t\bar{t}b\bar{b}$ : anatomy of full off-shell effects at differential level

- Off-shell effects amount to few permille for most observables used in SM analyses
- **Threshold observables** used in BSM studies are naturally more sensitive:

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [Phys. Rev. D \(107\) 2023](#)]



$$LO_{NWA} \rightarrow M_{\min}(e^+b) < \sqrt{m_t^2 - m_W^2} \approx 153 \text{ GeV}$$

$$M_{T2}(t) = \min_{\sum p_T^{\nu_i} = p_T^{miss}} \left[ \max \left\{ M_T^2(p_T(e^+ X_t), p_T(\nu_1)), M_T^2(p_T(\mu^- X_{\bar{t}}), p_T(\nu_2)) \right\} \right]$$

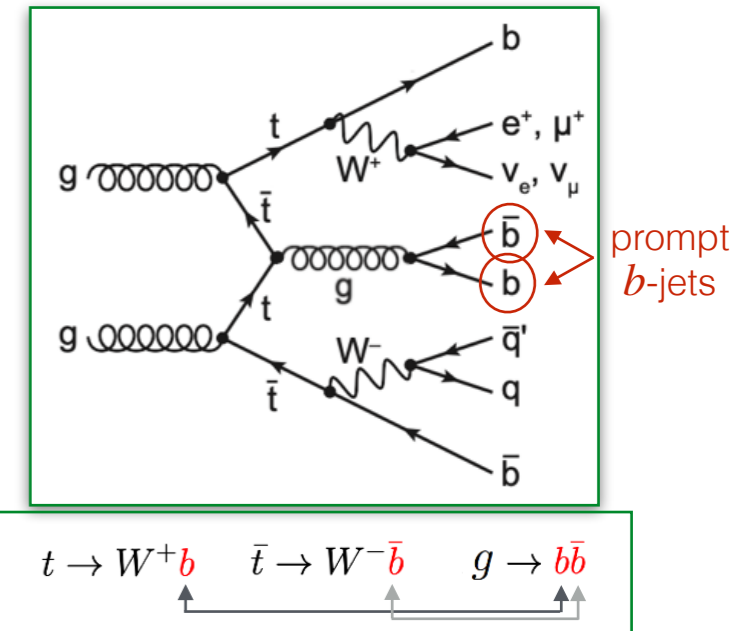
### III. Identification of prompt $b$ -jets

# $t\bar{t}b\bar{b}$ : prompt $b$ -jet identification

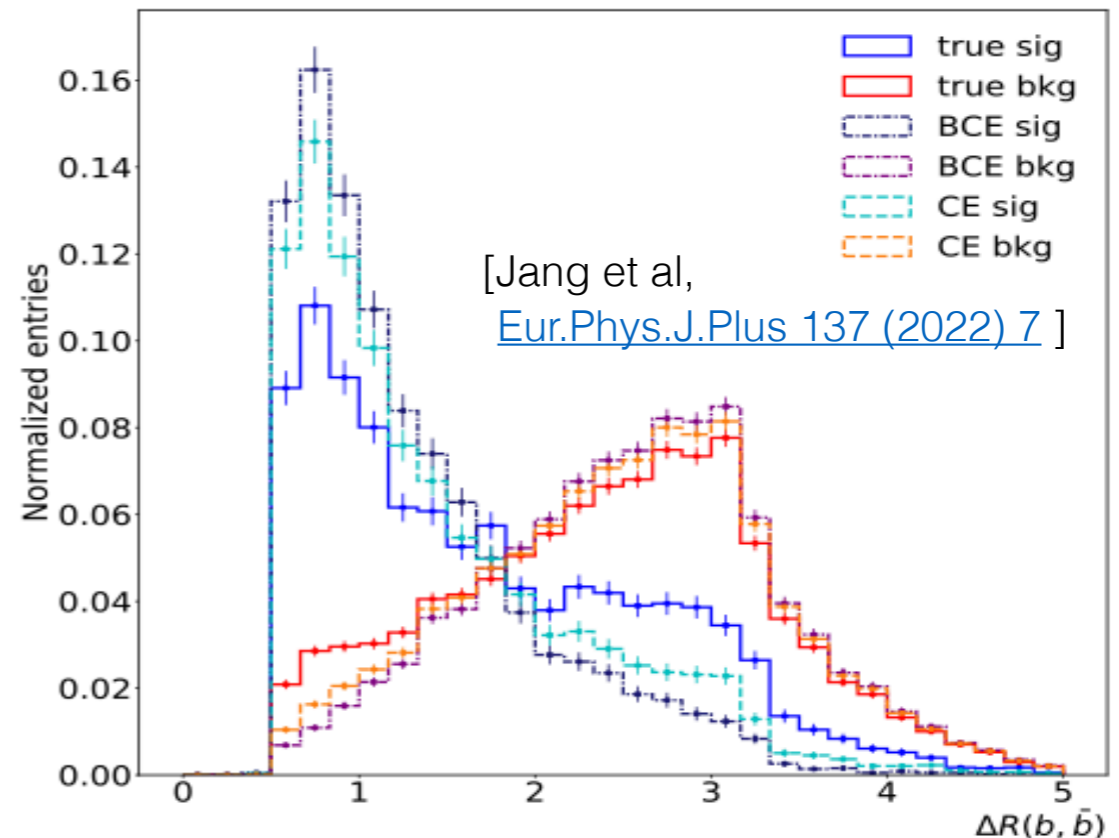
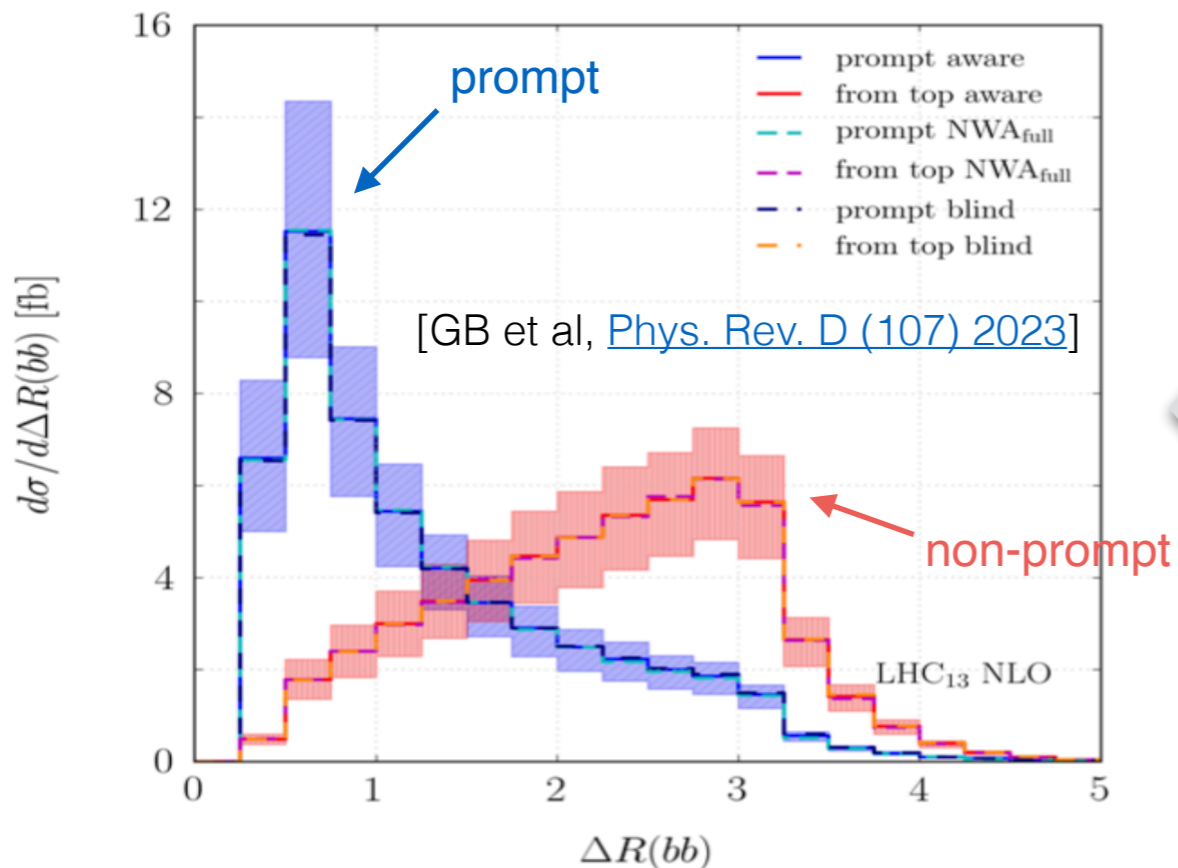
- Labelling prompt  $b$ -jets in  $t\bar{t}b\bar{b}$  is not free of ambiguities in a full calculation (due to combinatorial background and quantum interference)

- **Kinematic-based prescription:** determine prompt  $b$ -jets according to a **minimum principle** for  $Q$ :

$$Q = |M(t) - m_t| \times |M(\bar{t}) - m_t| \times |M^{\text{prompt}}(bb)|$$



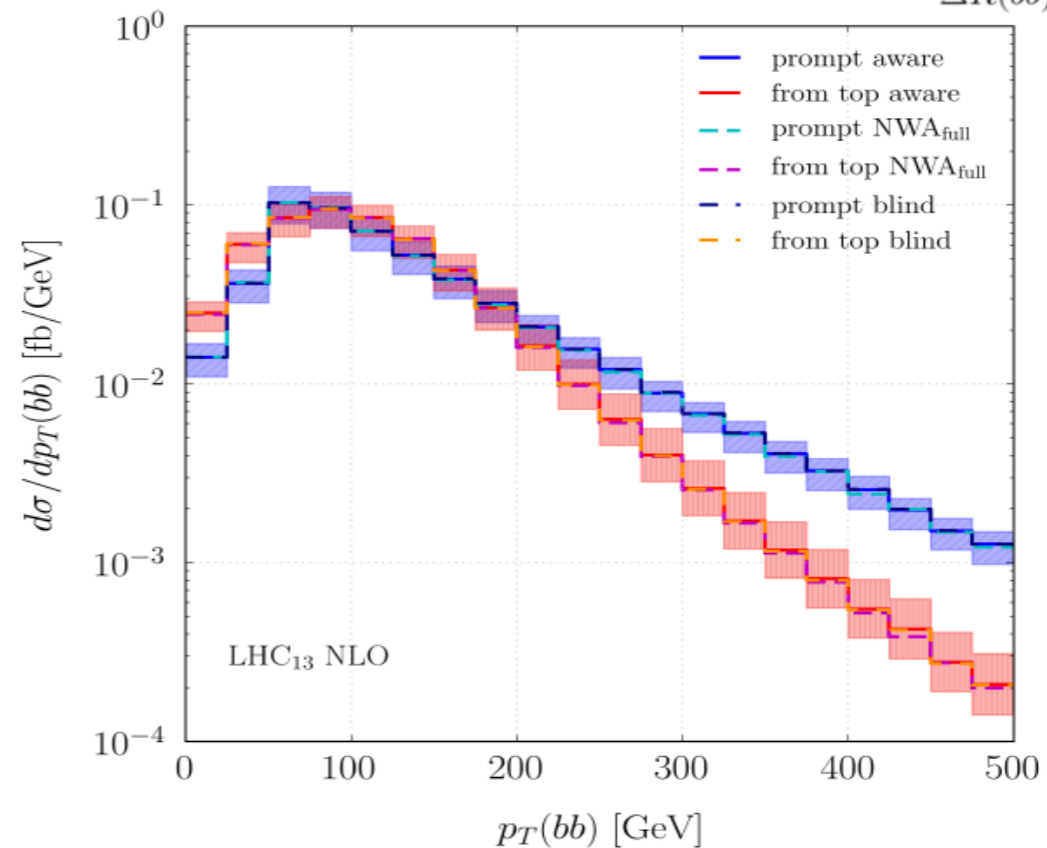
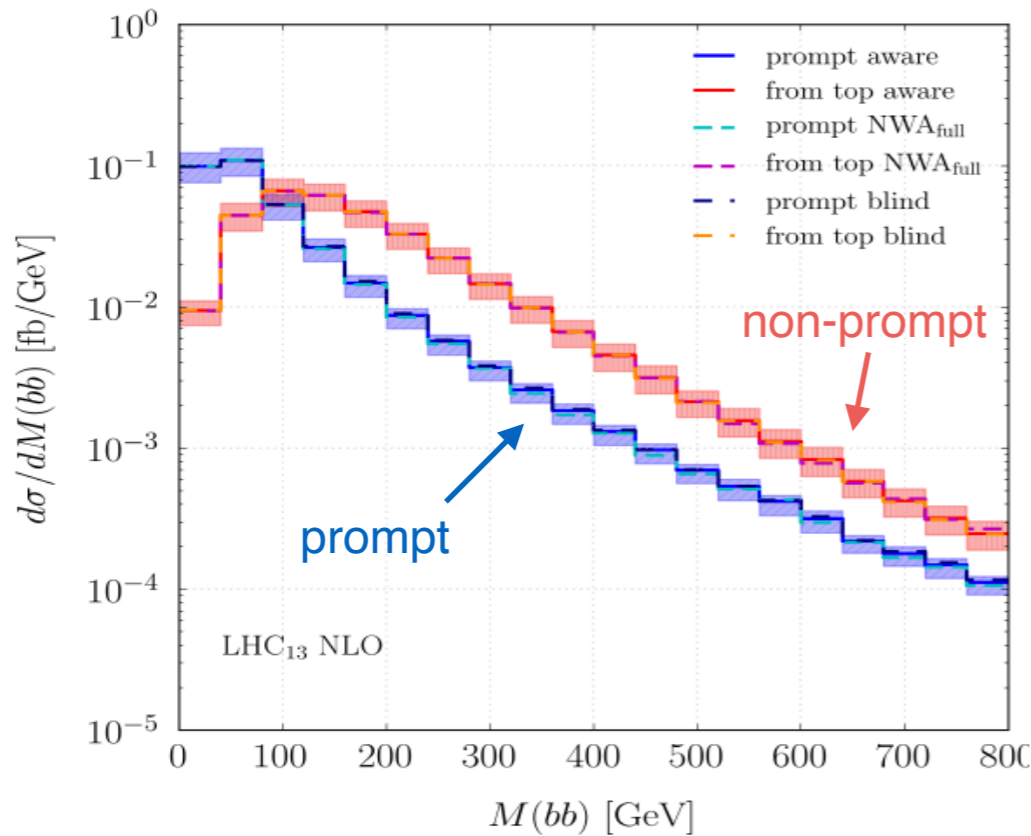
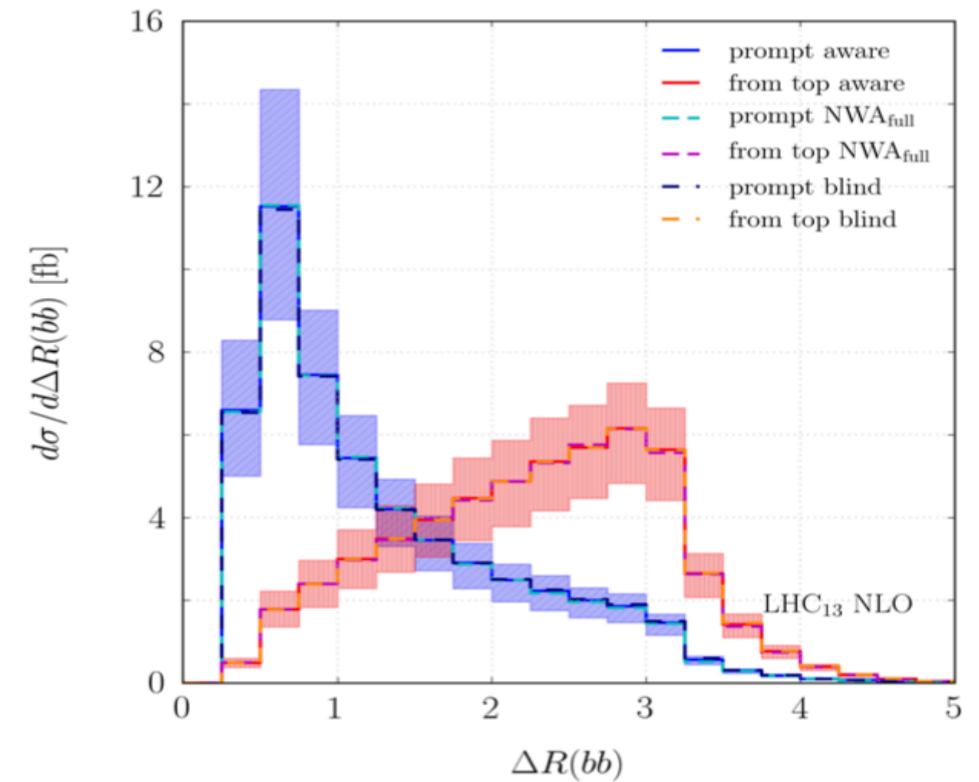
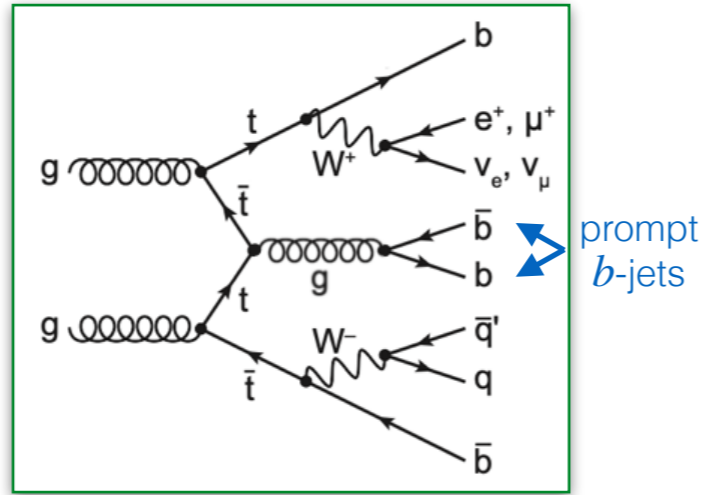
- Results consistent with DNN-based studies:



# $t\bar{t}b\bar{b}$ : prompt $b$ -jet identification

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [Phys. Rev. D \(107\) 2023](#)]

- Kinematical differences between  $b\bar{b}$  pairs belonging to **prompt** and **non-prompt** categories



## Summary

- Fixed-order analysis of based on *off-shell*  $pp \rightarrow t\bar{t}b\bar{b}$  (dilepton signatures)
  - QCD corrections are large
  - Dominant uncertainties at NLO:  $\mathcal{O}(20\%)$  [scale]
- Systematic comparison with NWA at different levels of accuracy
  - Off-shell effects small for most distributions used in SM analyses:  $\mathcal{O}(0.5\%)$
  - Impact of QCD corrections to top quark decays:  $-7\%$
  - Impact of  $\mathcal{O}(\alpha_s^2)$  effects in  $\sigma_{\text{NWA}}^{\text{NLO}}$  and  $\sigma_{\text{off-shell}}^{\text{NLO}}$  :  $6\%$  (within the scale uncertainties)
- Kinematic-based method for prompt  $b$ -jet labelling and top-quark reconstruction

## Outlook

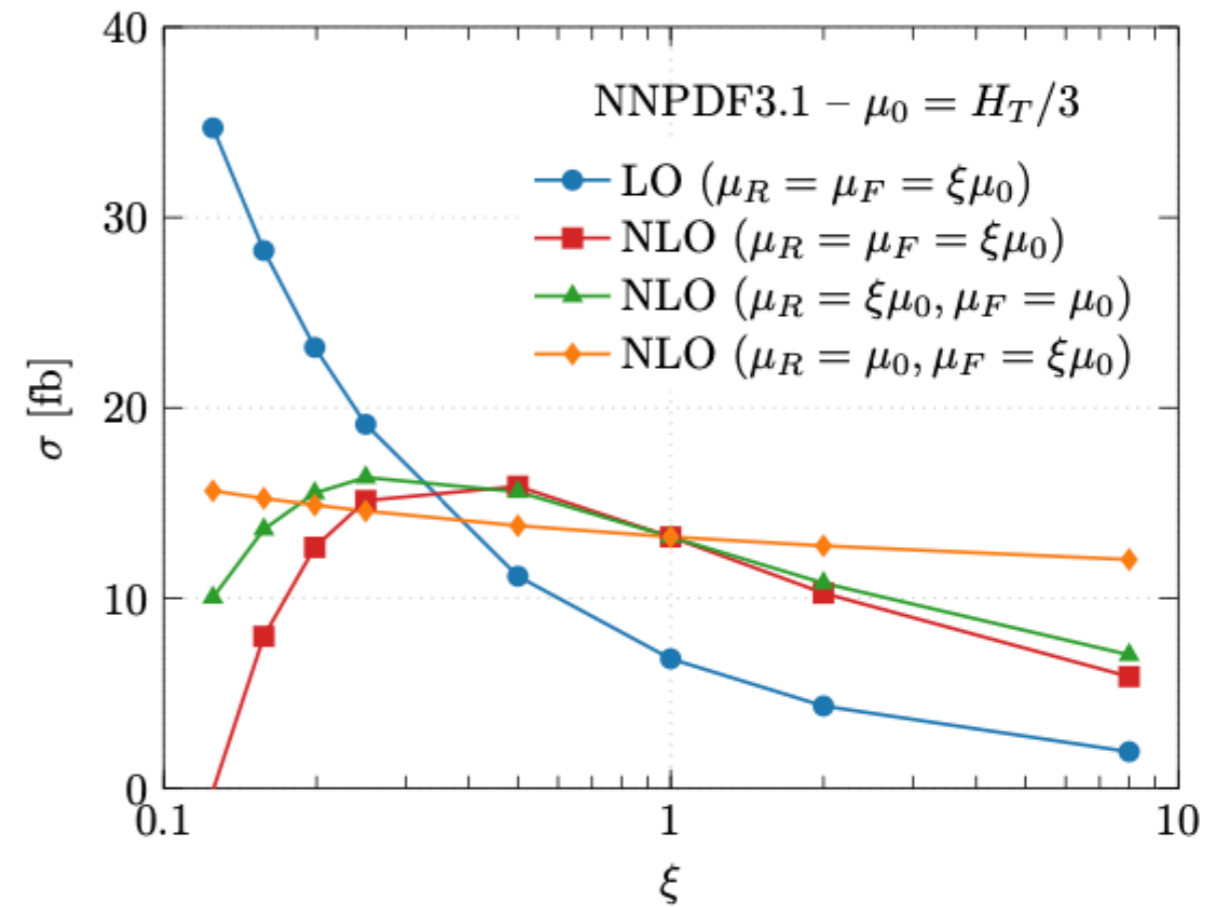
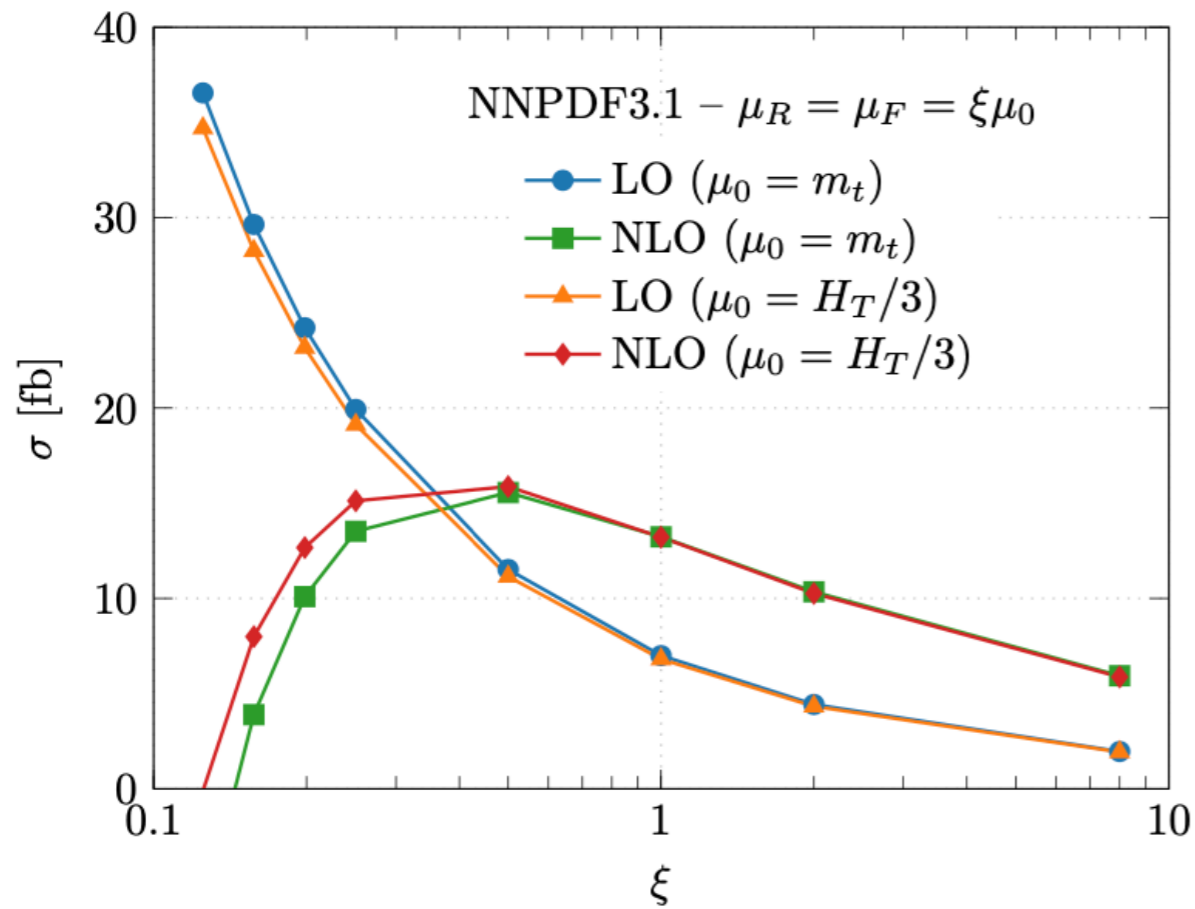
- Comparison with LHC data at differential level based on off-shell predictions

Backup slides



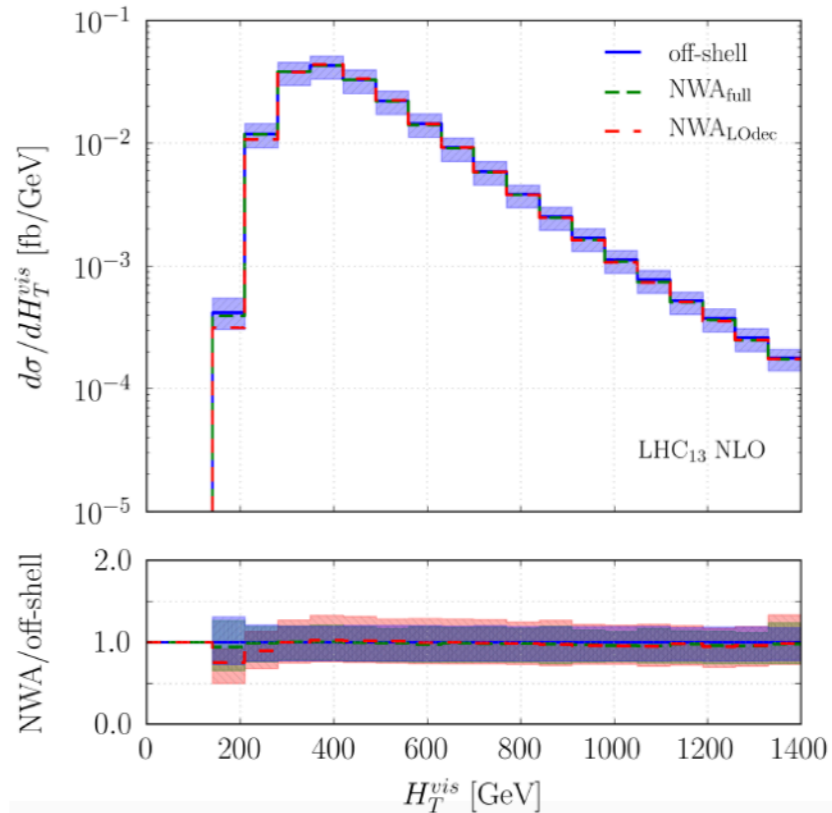
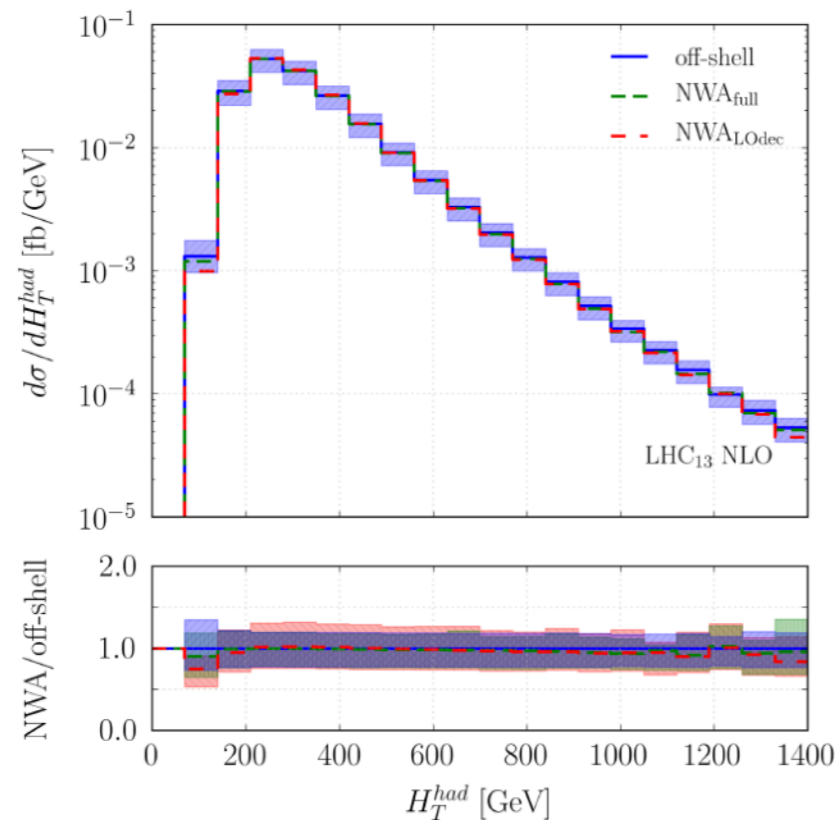
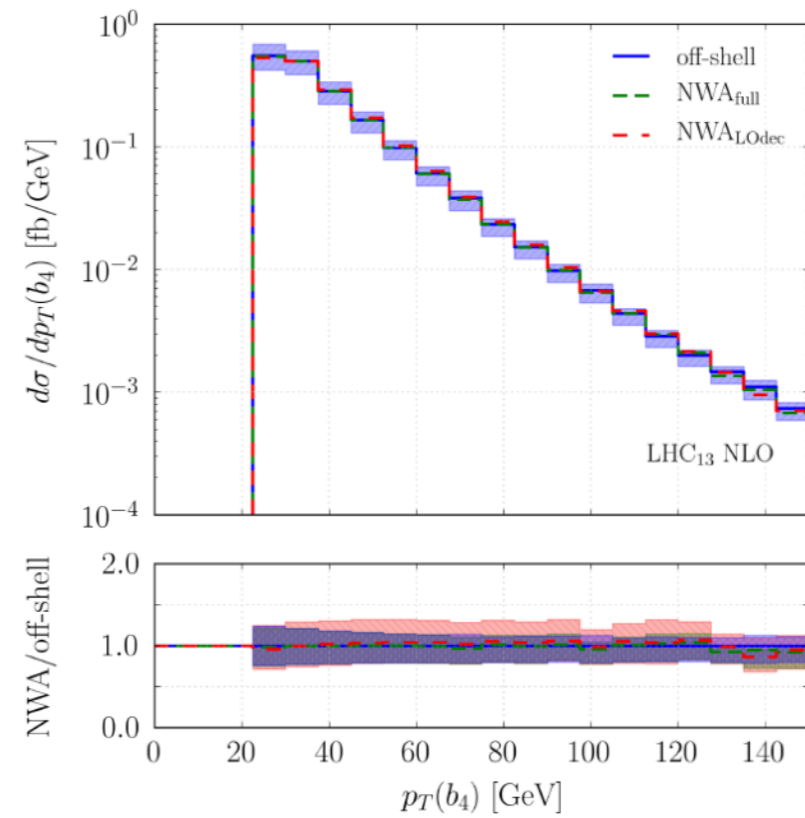
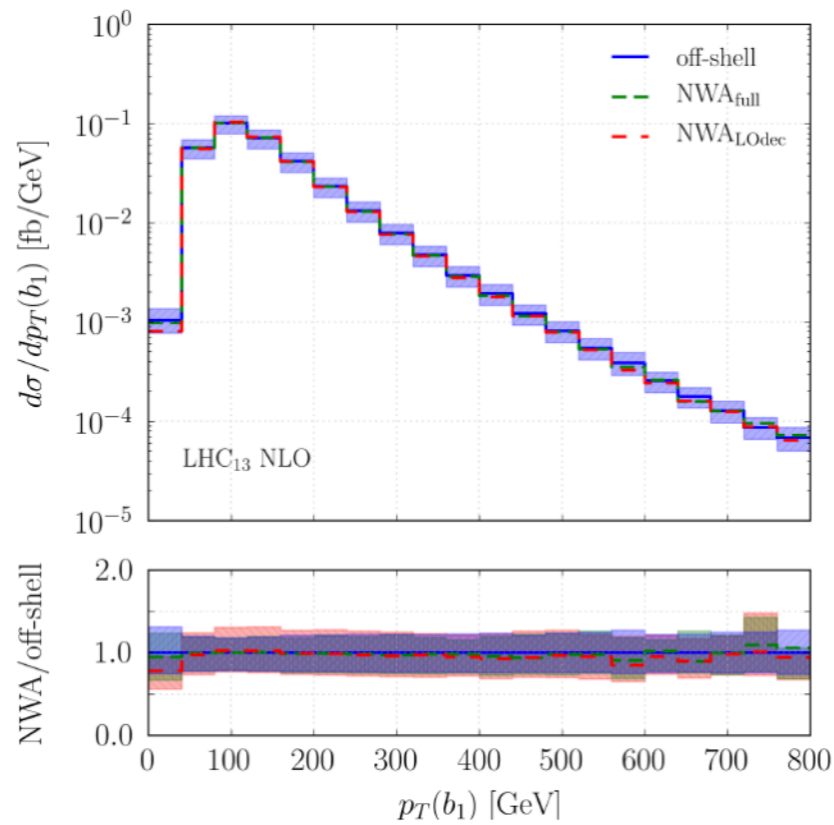
# $t\bar{t}b\bar{b}$ : scale dependence of the integrated cross section

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [JHEP 08 \(2021\) 008](#)]



# $t\bar{t}b\bar{b}$ : impact of off-shell effects at differential level

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [Phys. Rev. D \(107\) 2023](#)]



$$H_T^{had} = \sum_{i=1}^4 p_T(b_i)$$

$$H_T^{vis} = H_T^{had} + \sum_{i=1}^2 p_T(l_i)$$

# $t\bar{t}b\bar{b}$ : impact of initial-state $b$ quark contributions

- Contributions induced by initial state  $b$ -quarks are suppressed by PDFs
- How good is the approximation of neglecting  $b$ -initiated contributions ?

Born

$$\begin{aligned} b\bar{b} &\rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b}, \\ bb &\rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} bb \\ \bar{b}\bar{b} &\rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu \bar{b}\bar{b} \bar{b}\bar{b}. \end{aligned}$$

Real

$$\begin{aligned} gb &\rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} b & bb &\rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} bb g \\ g\bar{b} &\rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} \bar{b} & \bar{b}\bar{b} &\rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu \bar{b}\bar{b} \bar{b}\bar{b} g \\ b\bar{b} &\rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} g \end{aligned}$$

- Comparing two different approaches of identifying  $b$ -jets:

“Charge blind”



Cannot distinguish  
 $b$ - from  $\bar{b}$ -jets

vs

“Charge aware”

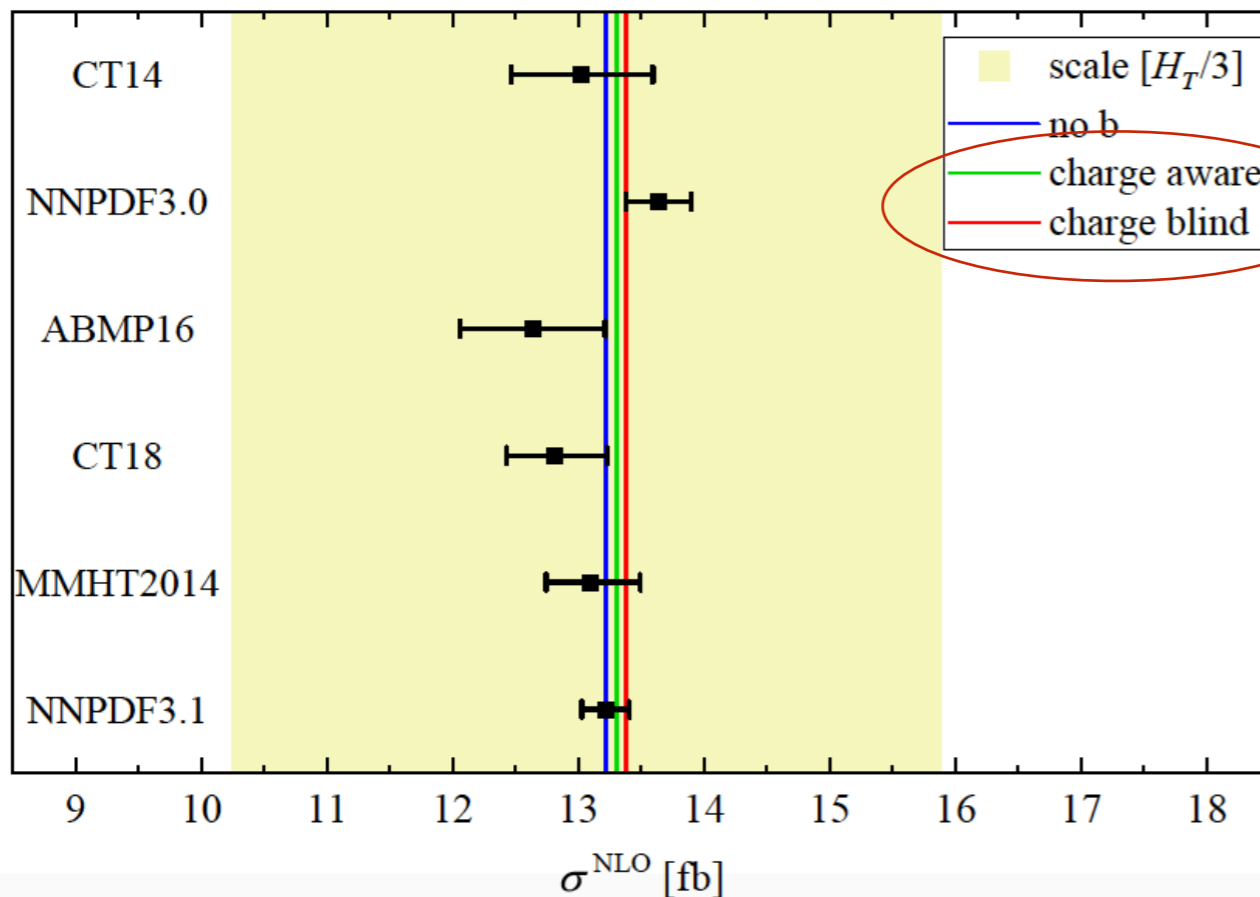
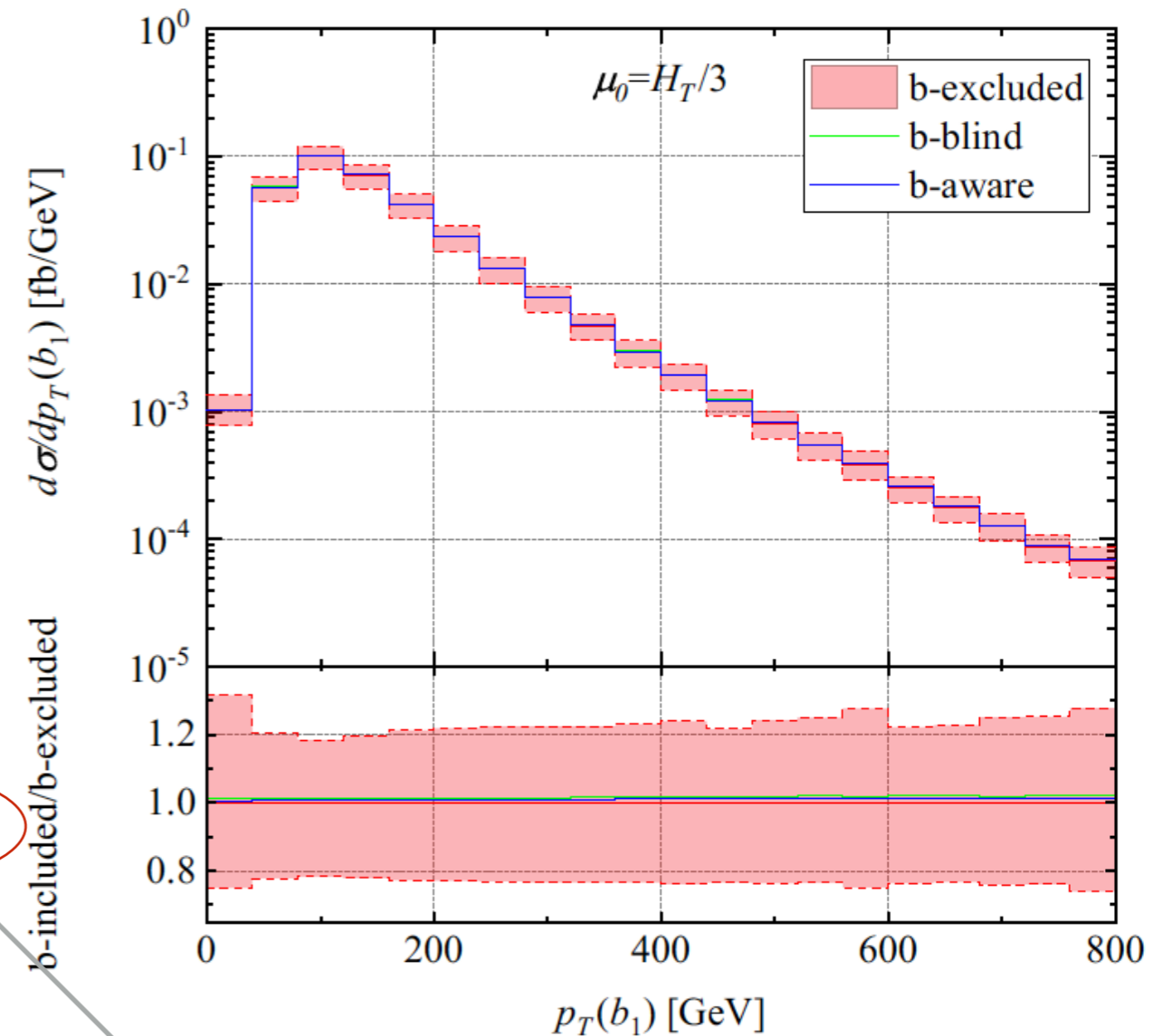
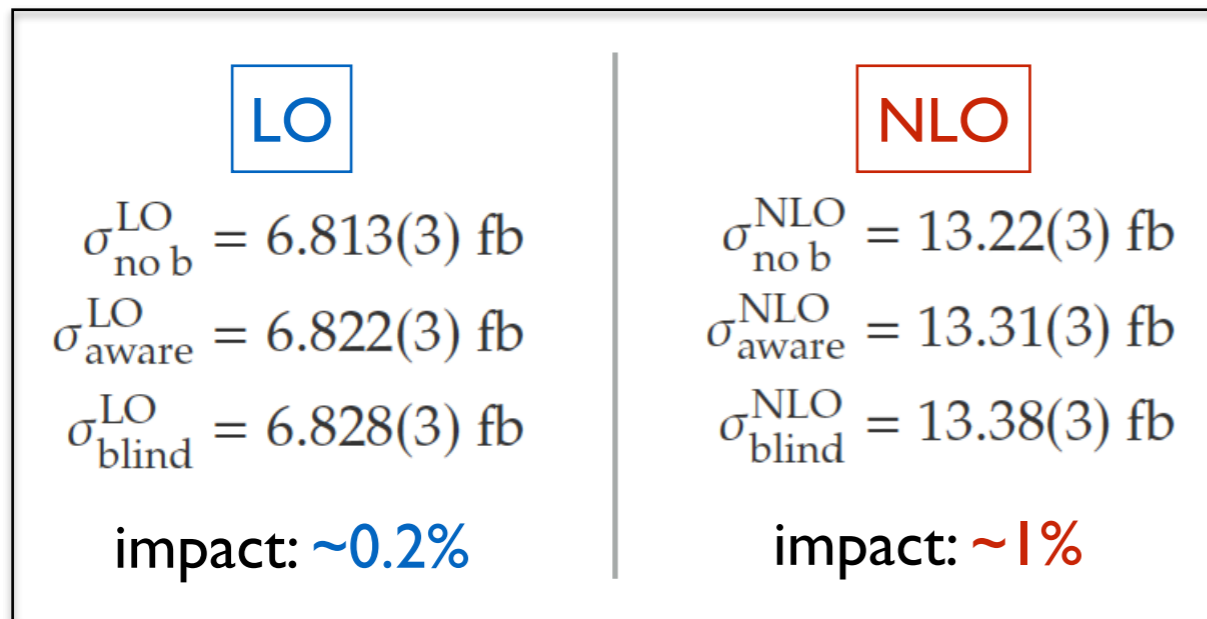


Can distinguish  
 $b$ - from  $\bar{b}$ -jets

[see e.g. [ATLAS-CONF-2018-022](#)]

# $t\bar{t}b\bar{b}$ : impact of initial-state $b$ quark contributions

[GB, Bi, Hartanto, Kraus, Lupattelli and Worek, [JHEP 08 \(2021\) 008](#)]



b-included/b-excluded

**“Charge blind”** vs **“Charge aware”**

↓

Cannot distinguish  $b$ - from  $\bar{b}$ -jets

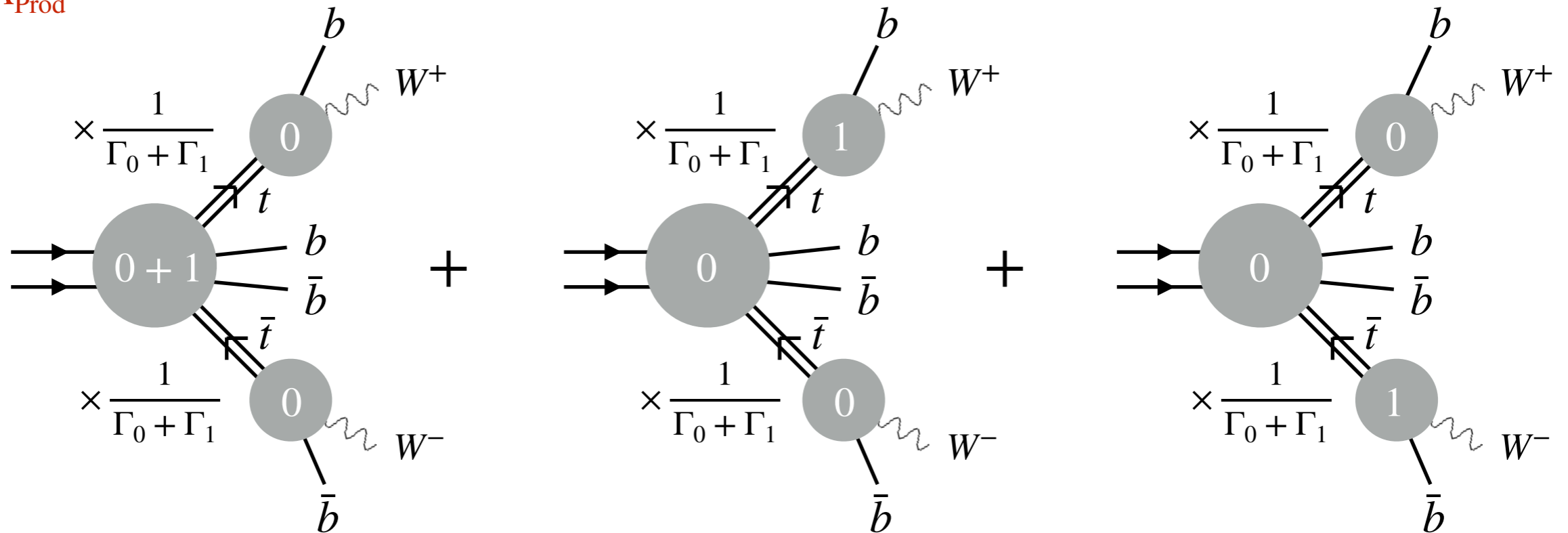
↓

Can distinguish  $b$ - from  $\bar{b}$ -jets

# Effects of $\Gamma_t$ expansion in NWA

- "Unexpanded" cross section in NWA:

$$d\sigma_{\text{NWA}_{\text{Prod}}}^{\text{NLO}} \equiv$$



- $d\sigma_{\text{NWA}_{\text{Prod}}}^{\text{NLO}}$  yields the same  $\Gamma_t^{\text{NLO}}$  factors that are present in the full off-shell calculation
- Most suitable setup to assess the impact of genuine off-shell effects

# Effects of $\Gamma_t$ expansion in NWA

- “Unexpanded” cross section in NWA:

$$\Gamma_t^{NLO} = \Gamma_0 + \Gamma_1$$

$\downarrow$                        $\downarrow$   
 $\mathcal{O}(\alpha_s^0)$      $\mathcal{O}(\alpha_s)$

$$\int d\sigma_{\text{NWA Prod}}^{NLO} =$$

The diagram illustrates the expansion of the NWA cross section into three terms, each representing a different order of the top quark width  $\Gamma_t$  expansion. The central vertex is labeled  $0+1$ ,  $0$ , or  $0$  respectively. The external vertices are labeled  $0$ ,  $1$ , or  $0$  and  $1$  respectively. The terms are summed together.

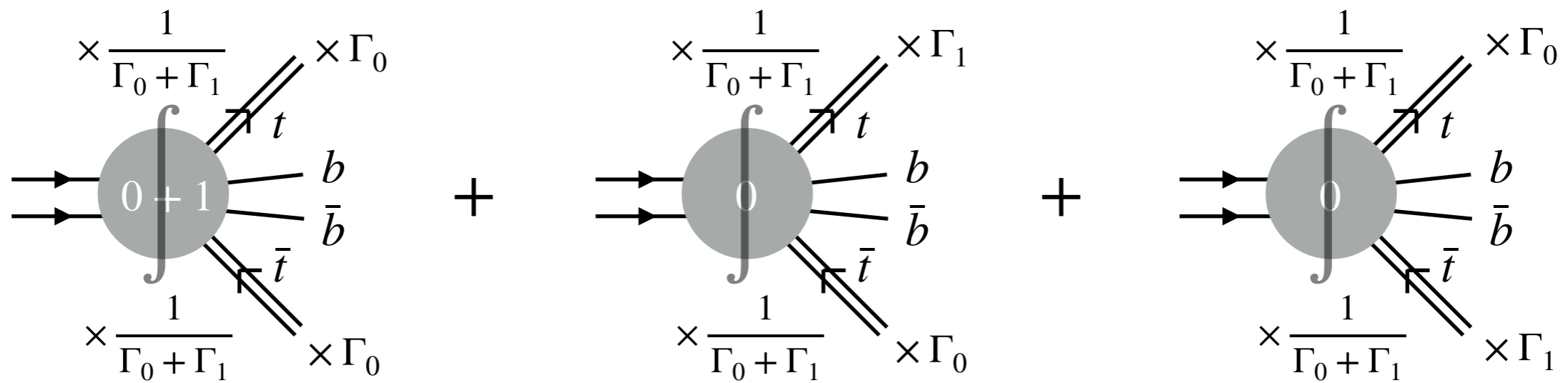
# Effects of $\Gamma_t$ expansion in NWA

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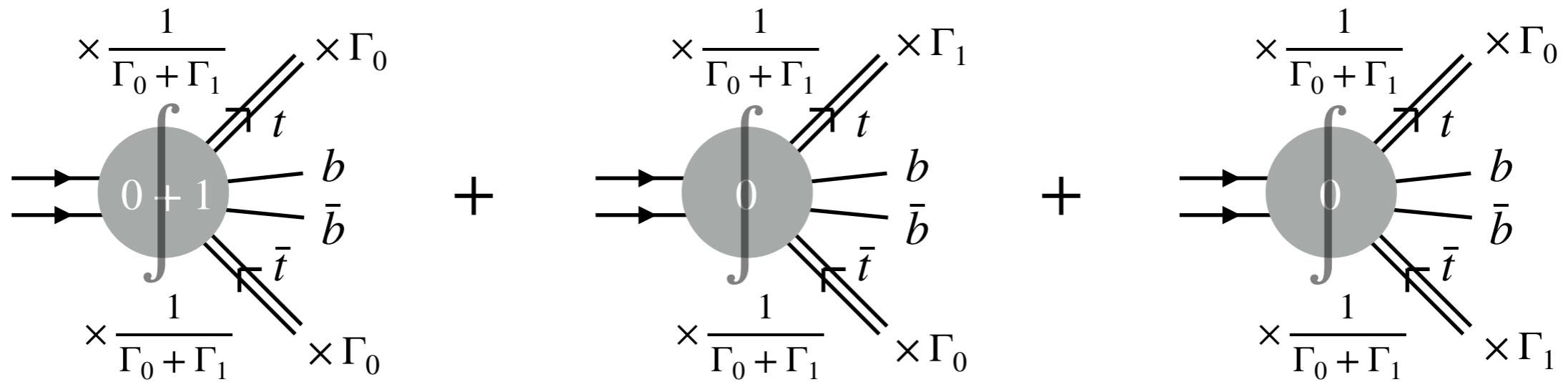
# Effects of $\Gamma_t$ expansion in NWA

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$\downarrow$                        $\downarrow$   
 $\mathcal{O}(\alpha_s^0)$      $\mathcal{O}(\alpha_s)$

$$\int d\sigma_{\text{NWA Prod}}^{NLO} =$$



$$= \int d\sigma_{\text{NWA Prod}}^{NLO} + \mathcal{O}(\alpha_s^2) = \sigma_{t\bar{t}b\bar{b}, \text{incl.}}^{NLO} + \mathcal{O}(\alpha_s^2)$$

- Rigorous factorization at NLO spoiled by *formally suppressed  $\mathcal{O}(\alpha_s^2)$  terms.*

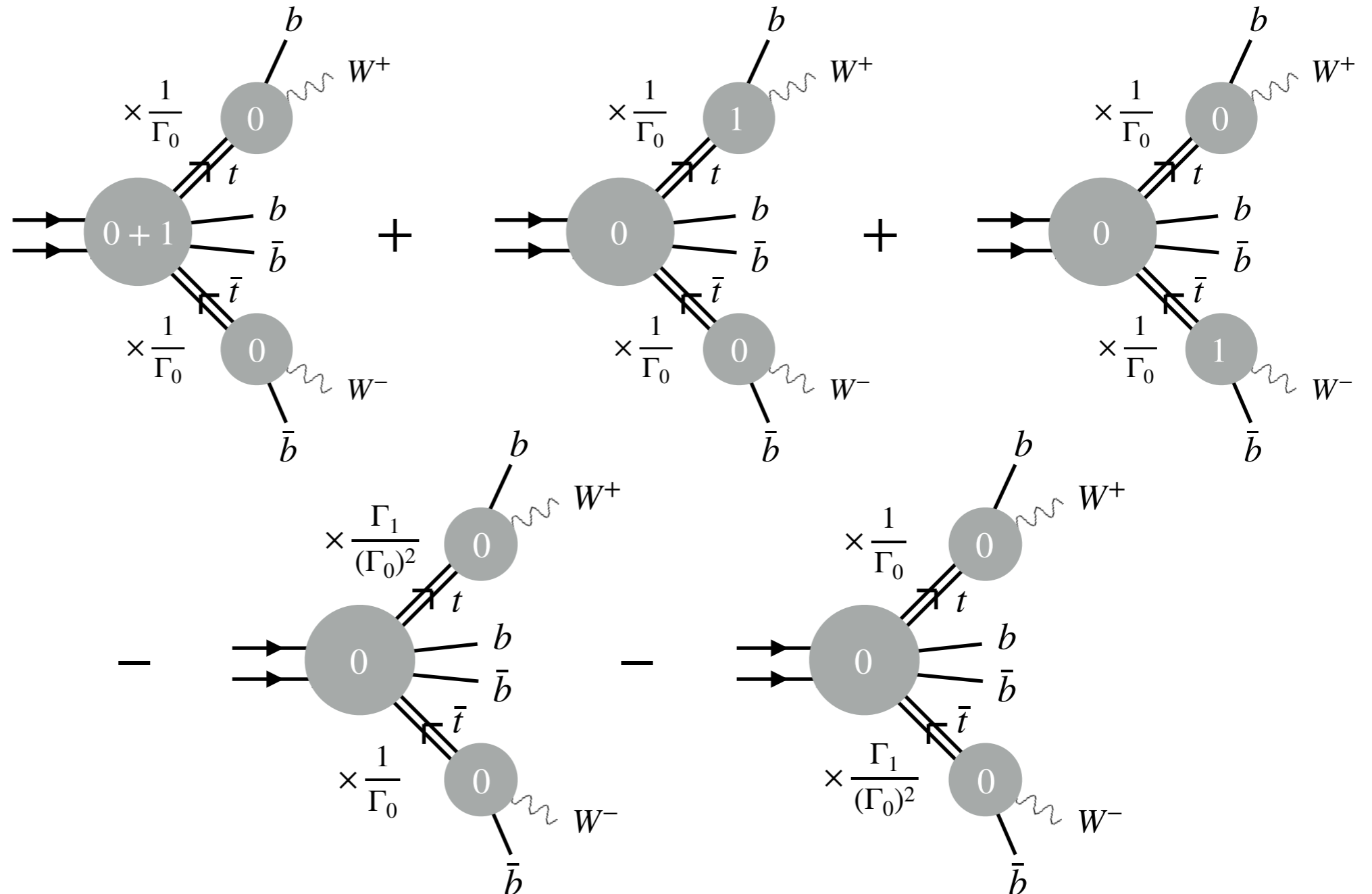


# Effects of $\Gamma_t$ expansion in NWA

- **“Expanded”** cross section in NWA:

$$\frac{1}{\Gamma_0 + \Gamma_1} \sim \frac{1}{\Gamma_0} - \frac{\Gamma_1}{(\Gamma_0)^2} + \mathcal{O}(\alpha_s^2)$$

$d\sigma_{\text{NWA Prod, exp}}^{\text{NLO}} \equiv$



# Effects of $\Gamma_t$ expansion in NWA

- "Expanded" cross section in NWA:

$$\frac{1}{\Gamma_0 + \Gamma_1} \sim \frac{1}{\Gamma_0} - \frac{\Gamma_1}{(\Gamma_0)^2} + \mathcal{O}(\alpha_s^2)$$

$$\int d\sigma_{\text{NWA Prod, exp}}^{\text{NLO}} =$$

The expansion of the NWA cross section is shown as a sum of five diagrams. The first row contains three diagrams, and the second row contains two diagrams, all separated by plus and minus signs. Each diagram features a central vertex and two side vertices. The central vertex is labeled '0+1' in the first diagram and '0' in the others. The side vertices are labeled '0' or '1'. Factors of  $1/\Gamma_0$  and  $\Gamma_1/(\Gamma_0)^2$  are associated with the diagrams. The diagrams represent the expansion of the cross section in the narrow width approximation (NWA) for top quark production and decay.

# Effects of $\Gamma_t$ expansion in NWA

- "Expanded" cross section in NWA:

$$\frac{1}{\Gamma_0 + \Gamma_1} \sim \frac{1}{\Gamma_0} - \frac{\Gamma_1}{(\Gamma_0)^2} + \mathcal{O}(\alpha_s^2)$$

$$\int d\sigma_{\text{NWA Prod, exp}}^{NLO} =$$

The diagrammatic expansion shows the following terms:

- Term 1:  $\int d\sigma_{\text{NWA Prod, exp}}^{NLO} \times \frac{1}{\Gamma_0} \times \Gamma_0$
- Term 2:  $\int d\sigma_{\text{NWA Prod, exp}}^{NLO} \times \frac{1}{\Gamma_0} \times \Gamma_1$
- Term 3:  $\int d\sigma_{\text{NWA Prod, exp}}^{NLO} \times \frac{1}{\Gamma_0} \times \Gamma_0$
- Term 4:  $\int d\sigma_{\text{NWA Prod, exp}}^{NLO} \times \frac{\Gamma_1}{(\Gamma_0)^2} \times \Gamma_0$
- Term 5:  $\int d\sigma_{\text{NWA Prod, exp}}^{NLO} \times \frac{1}{\Gamma_0} \times \frac{\Gamma_1}{(\Gamma_0)^2} \times \Gamma_0$

# Effects of $\Gamma_t$ expansion in NWA

- "Expanded" cross section in NWA:

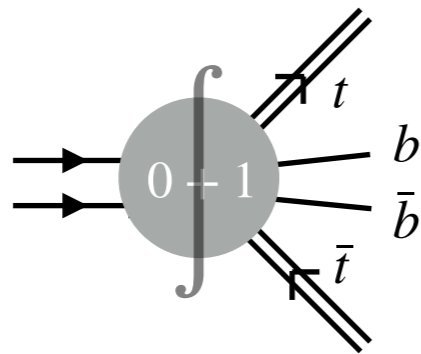
$$\frac{1}{\Gamma_0 + \Gamma_1} \sim \frac{1}{\Gamma_0} - \frac{\Gamma_1}{(\Gamma_0)^2} + \mathcal{O}(\alpha_s^2)$$

$$\int d\sigma_{\text{NWA Prod, exp}}^{NLO} =$$

The diagrammatic expansion shows the NWA cross section as a sum of terms. The first term is the tree-level NWA cross section, represented by a circle with a top quark propagator, multiplied by  $\frac{1}{\Gamma_0}$  and  $\Gamma_0$ . The second term is the NWA cross section with a top quark propagator, multiplied by  $\frac{1}{\Gamma_0}$  and  $\Gamma_1$ . The third term is the NWA cross section with a top quark propagator, multiplied by  $\frac{1}{\Gamma_0}$  and  $\Gamma_0$ . The fourth term is the NWA cross section with a top quark propagator, multiplied by  $\frac{\Gamma_1}{(\Gamma_0)^2}$  and  $\Gamma_0$ . The fifth term is the NWA cross section with a top quark propagator, multiplied by  $\frac{1}{\Gamma_0}$  and  $\Gamma_0$ .

# Effects of $\Gamma_t$ expansion in NWA

$$\int d\sigma_{\text{NWA Prod, exp}}^{\text{NLO}} =$$



$$\equiv \sigma_{t\bar{t}b\bar{b}, \text{incl.}}^{\text{NLO}}$$

- Rigorous expansion of  $\Gamma_t^{\text{NLO}}$  in NWA gets rid of “spurious”  $\mathcal{O}(\alpha_s^2)$  contributions
- Note: the same procedure does not apply straightforwardly to the off-shell calculation

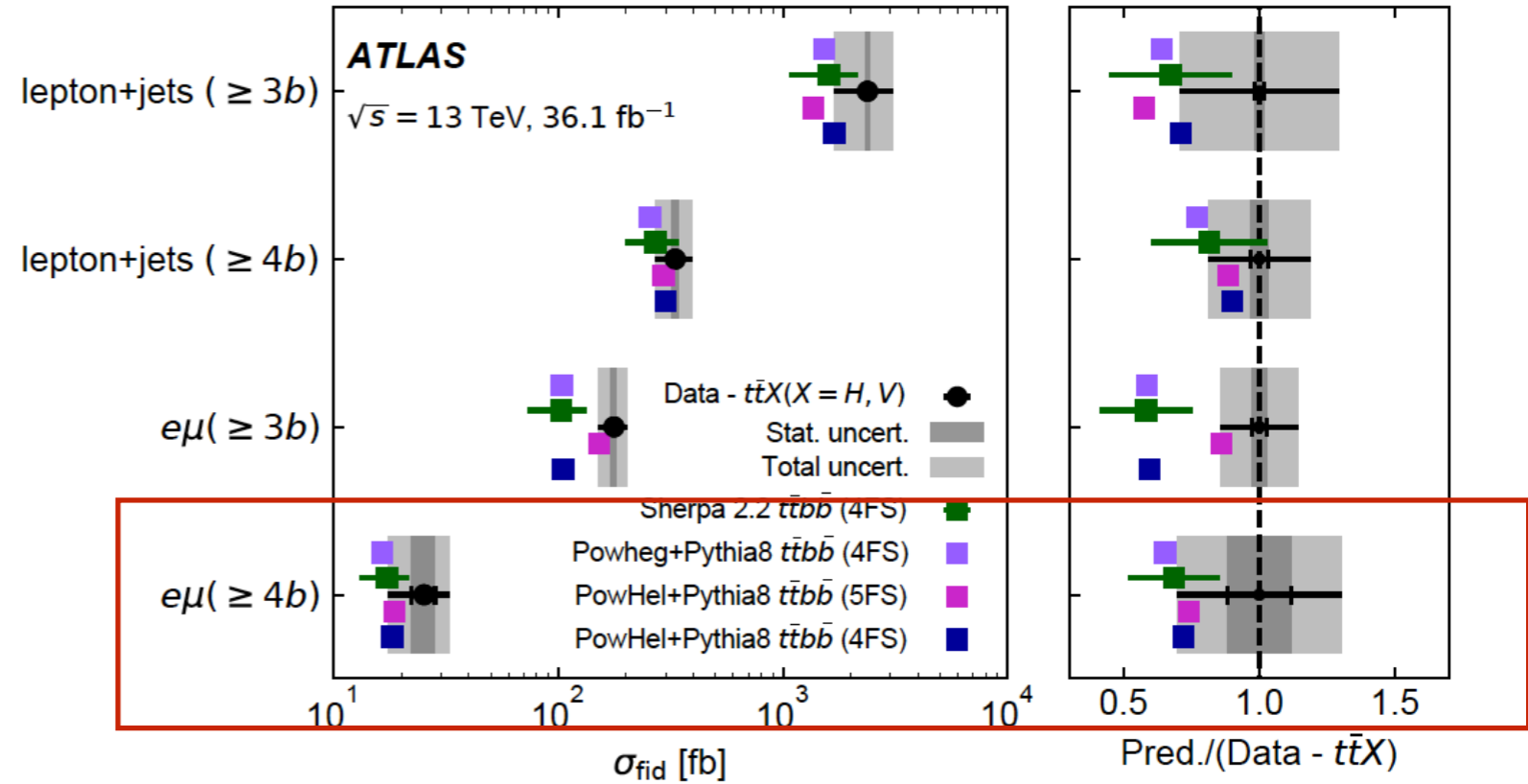
- The unusually large size of  $\mathcal{O}(\alpha_s^2)$  effects,  $\mathcal{O}(6\%)$ , relates to the large size of QCD corrections to  $t\bar{t}b\bar{b}$  production cross section
- These effects are well within the NLO scale uncertainties,  $\mathcal{O}(20\%)$

ATLAS cuts:

$$p_T(\ell) > 25 \text{ GeV}, \quad p_T(b) > 25 \text{ GeV},$$

$$|y(\ell)| < 2.5, \quad |y(b)| < 2.5,$$

$$\Delta R(bb) > 0.4, \quad \Delta R(\ell b) > 0.4,$$



[ATLAS, [JHEP 04 \(2019\) 046](#)]

Theoretical predictions	$\sigma_{e\mu+4b}$ [fb]
SHERPA+OPENLOOPS (4FS)	$17.2 \pm 4.2$
POWHEG-BOX+PYTHIA 8 (4FS)	16.5
POWHEL+PYTHIA 8 (5FS)	18.7
POWHEL+PYTHIA 8 (4FS)	18.2
Experimental result (ATLAS)	$25 \pm 6.5$

[GB et al, [JHEP 08 \(2021\) 008](#)]

**HELAC-NLO (5FS):  $20.0 \pm 4.3$  fb**